# BLACK SWANS AND THE MANY SHADES OF UNCERTAINTY

Nicholas Kozeniauskas Anna Orlik<sup>1</sup> Laura Veldkamp NYU Fed Board NYU Stern

Winter Meeting of the Econometric Society

3rd January 2016

<sup>&</sup>lt;sup>1</sup>Disclaimer: The views expressed herein are those of the authors and do not necessarily reflect the position of the Board of Governors of the Federal Reserve or the Federal Reserve System.

# Types of Uncertainty



VIX: expected future variance of S&P 500 Micro uncertainty: IQR of firm sales growth (MicroU) Higher-order uncertainty: std. of GDP growth forecasts (HiOrderU)

# Introduction

- Approaches to modeling uncertainty
  - MacroU: heteroskedastic aggregate shock
  - MicroU: heteroskedastic firm-specific shock
  - HiOrderU: changes in dispersion of private information

Provides no connection between different types of uncertainty

- In the paper: the different types of uncertainty are highly correlated—even after controlling for the business cycle
- Why? What's the connection between the various uncertainty shocks?

### Skewness amplifies uncertainty in bad times



MacroU: average st. dev. of beliefs about TFP growth

Skewness amplifies MacroU in bad times

### Skewness amplifies uncertainty in bad times



Same force amplifies disagreement when uncertainty is high

- $\rightarrow$  Firms choose different inputs  $\rightarrow$  growth dispersion (MicroU)
- & Firms make different GDP growth forecasts (HiOrderU)

### Skewness amplifies uncertainty in bad times



Key: With skewness, good times are more similar than bad times

#### Model

- Islands model with unit mass of islands/firms
- Decision: choose labor supply to maximize utility

$$egin{aligned} U_{it} &= oldsymbol{Q}_{it} - L^{\gamma}_{it}, \ oldsymbol{Q}_{it} &= oldsymbol{A}_t L_{it} \end{aligned}$$

TFP process:

$$\Delta a_t \equiv \Delta \log A_t = c + b \exp X_t$$

 $X_t$  : GARCH(1,1), parameters unknown

- Firms forecast  $X_t$  at end of t 1 to choose labor
  - Prior for *t*: estimate GARCH model on data to t 1.
  - Posterior: prior + idiosyncratic signal by Bayes' law.

$$\begin{aligned} \mathbf{Z}_{i,t-1} &= \Delta \mathbf{X}_t + \eta_{t-1} + \psi_{i,t-1}, \\ \eta_{t-1} &\sim \mathbf{N}(\mathbf{0}, \sigma_{\eta}^2), \quad \psi_{i,t-1} \sim \mathbf{N}(\mathbf{0}, \sigma_{\psi}^2). \end{aligned}$$

### Model cont.

- Key ingredients of model
  - 1. Negatively skewed TFP growth: calibration  $\rightarrow b < 0$
  - 2. Variation in prior precision of beliefs about  $X_t$
  - 3. Private information
- Role of ingredients 2 and 3:

More uncertainty about aggregate state (more MacroU)

 $\rightarrow$  more weight on private information

 $\rightarrow$  more dispersed actions (MicroU) and forecasts (HiOrderU)

► Investigate role of skewness by comparing results to model with ∆a<sub>t</sub> = X<sub>t</sub>

## Quantitative exercise

- Calibration
  - Period: 1962Q3–2011Q4
  - ► TFP growth (5 params.) calibrated to moments of GDP growth
  - ► Signal noises calibrated to moments of GDP growth forecasts
- Uncertainty measures
  - MacroU: Av. std. of beliefs about TFP growth
  - ► HiOrderU: Cross-sectional st. dev. of GDP growth forecasts
  - MicroU: Cross-sectional IQR of firm level sales growth
- We want to explain
  - 1. Size of HiOrderU and MicroU shocks
  - 2. Correlation of HiOrderU and MicroU
  - 3. Correlation of HiOrderU and MicroU with GDP growth

	Model	Data
 (a) Micro Uno	certainty	
Std.	14.7	11.6
Corr. with GDP growth	-0.07	-0.52
 Corr. with HiOrderU	0.21	0.43
(b) HiOrder Un	certainty	
Std.	23.6	31.1
Corr. with GDP growth	-0.17	-0.28

	Model	Data
(a) Micro Unc	ertainty	
Std.	14.7	11.6
Corr. with GDP growth	-0.07	-0.52
Corr. with HiOrderU	0.21	0.43
(b) HiOrder Uncertainty		
Std.	23.6	31.1
Corr. with GDP growth	-0.17	-0.28

Generates most uncertainty shocks

	Model	Data
(a) Micro Unc	ertainty	
Std.	14.7	11.6
Corr. with GDP growth	-0.07	-0.52
Corr. with HiOrderU	0.21	0.43
(b) HiOrder Uncertainty		
Std.	23.6	31.1
Corr. with GDP growth	-0.17	-0.28

Generates most uncertainty shocks

Generates 1/2 of MicroU and HiOrderU correlation

	Model	Data
(a) Micro Unc	ertainty	
Std.	14.7	11.6
Corr. with GDP growth	-0.07	-0.52
Corr. with HiOrderU	0.21	0.43
(b) HiOrder Uncertainty		
Std.	23.6	31.1
Corr. with GDP growth	-0.17	-0.28

Generates most uncertainty shocks Generates 1/2 of MicroU and HiOrderU correlation Uncertainty countercyclical

	Model	Data
(a) Micro Unc	ertainty	
Std.	14.7	11.6
Corr. with GDP growth	-0.07	-0.52
Corr. with HiOrderU	0.21	0.43
(b) HiOrder Uncertainty		
Std.	23.6	31.1
Corr. with GDP growth	-0.17	-0.28

Generates most uncertainty shocks Generates 1/2 of MicroU and HiOrderU correlation Uncertainty countercyclical MicroU very countercyclical in the data

	No skewness	Full Model	
(a) Micro	(a) Micro Uncertainty		
Std.	4.7	14.7	
Corr. with GDP growth	0.00	-0.07	
Corr. with HiOrderU	0.16	0.21	
(b) HiOrder Uncertainty			
Std.	5.9	23.6	
Corr. with GDP growth	0.00	-0.17	

	No skewness	Full Model
(a) Micro	Uncertainty	
Std.	4.7	14.7
Corr. with GDP growth	0.00	-0.07
Corr. with HiOrderU	0.16	0.21
(b) HiOrder Uncertainty		
Std.	5.9	23.6
Corr. with GDP growth	0.00	-0.17

GARCH & param. learning  $\rightarrow$  uncertainty shocks

	No skewness	Full Model
(a) Micro Uncertainty		
Std.	4.7	14.7
Corr. with GDP growth	0.00	-0.07
Corr. with HiOrderU	0.16	0.21
(b) HiOrder Uncertainty		
Std.	5.9	23.6
Corr. with GDP growth	0.00	-0.17

GARCH & param. learning  $\rightarrow$  uncertainty shocks Skewness amplifies uncertainty shocks

	No skewness	Full Model	
(a) Micro	(a) Micro Uncertainty		
Std.	4.7	14.7	
Corr. with GDP growth	0.00	-0.07	
Corr. with HiOrderU	0.16	0.21	
(b) HiOrder Uncertainty			
Std.	5.9	23.6	
Corr. with GDP growth	0.00	-0.17	

GARCH & param. learning  $\rightarrow$  uncertainty shocks Skewness amplifies uncertainty shocks GARCH & param. learning  $\rightarrow$  corr. b/w MicroU and HiOrderU

	No skewness	Full Model
(a) Micro		
Std.	4.7	14.7
Corr. with GDP growth	0.00	-0.07
Corr. with HiOrderU	0.16	0.21
(b) HiOrder Uncertainty		
Std.	5.9	23.6
Corr. with GDP growth	0.00	-0.17

GARCH & param. learning  $\rightarrow$  uncertainty shocks Skewness amplifies uncertainty shocks GARCH & param. learning  $\rightarrow$  corr. b/w MicroU and HiOrderU Skewness generates countercycle uncertainty

### Conclusion

Recent research uses different kinds of uncertainty shocks

This paper: What's the connection between them?

We use some exogenous MacroU & explain MicroU and HiOrderU

- ► MacroU shocks  $\rightarrow$  agents vary their reliance on private info  $\rightarrow$  MicroU and HiOrderU shocks
- Negative skewness in aggregate outcomes
  - $\rightarrow$  good times are more similar than bad times
  - $\rightarrow$  MacroU, MicroU and HiOrderU amplified in bad times