

# Multidimensional Poverty Dynamics: Methodology And Results for 34 Countries

Sabina Alkire, José Manuel Roche and Ana Vaz

AEA, January, 2017

Session: Poverty, Shared Prosperity, and Vulnerability

Tabita, Kenya

Rabiya, India

Stéphanie, Madagascar

Agathe, Madagascar

Dalma, Kenya

Ann-Sophie, Kenya

Valérie, Madagascar



# Motivation

- This paper set out a systemic account of multidimensional poverty dynamic using the Alkire-Foster Adjusted Headcount Ratio and its consistent sub-indices.
- It also scrutinizes three approaches to assessing the pro-pooriness of multidimensional poverty reduction.
- These technics were then applied to the analysis of changes in multidimensional poverty based on the Global MPI and related destitution measure.

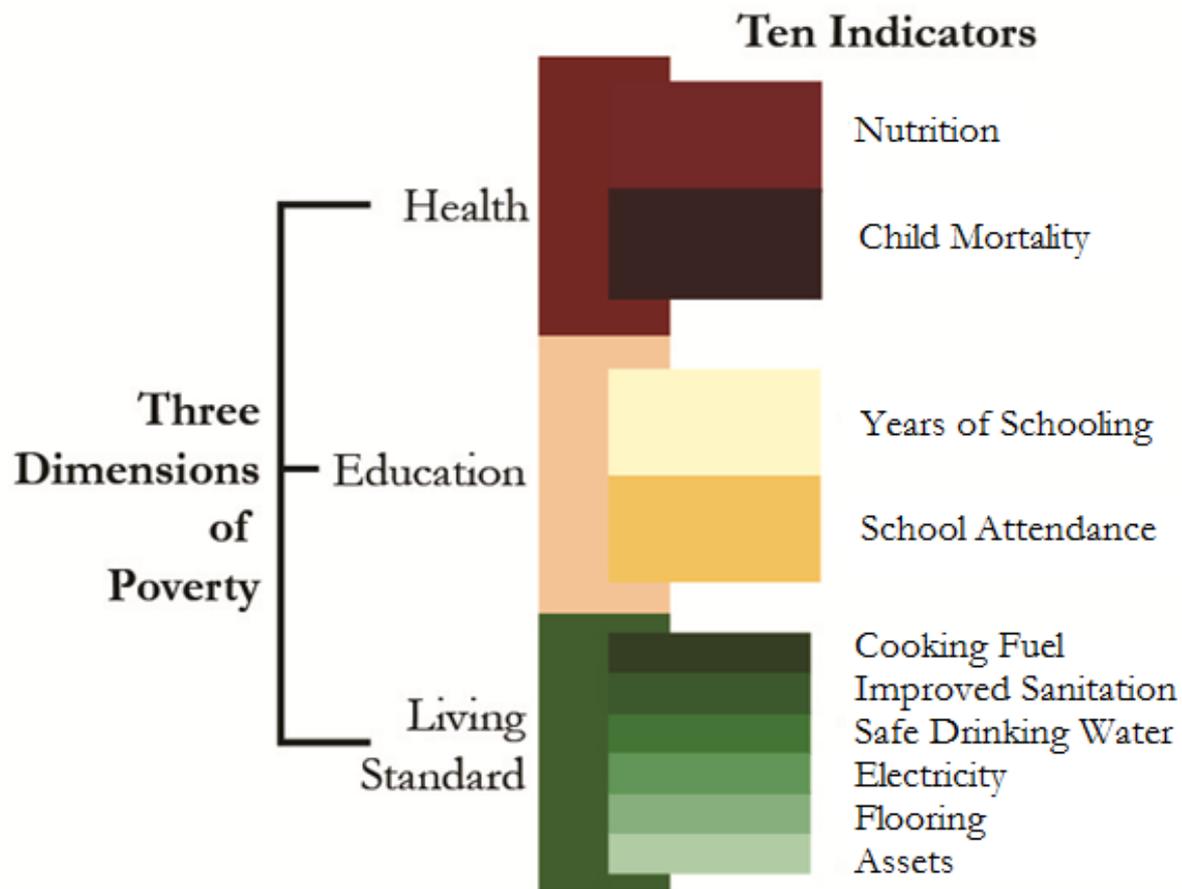
# What is the MPI?

- The MPI is an internationally comparable index of acute poverty for 100+ developing countries.
- It was launched in 2010 in the *Human Development Report*, and updated in 2011, 2013 and 2014.
- The MPI methodology is being adapted for national poverty measures – using better indicators for that policy context.

# Data: DHS surveys

- Coverage – poverty dynamics in this paper:
  - 34 countries
  - 338 sub-national regions + disaggregation for ethnic groups for Benin, Kenya and Ghana
  - Roughly 2.5 billion people (2010); on aggregate like Haiti.
- Comparisons across time are as strict as data permit.
- Survey years and intervals vary (2 to 12 years – 30 periods are 4 to 7 years, and for 20 countries most recent data are 2010-12).
- 29 countries have all 10 indicators; 5 have 9 indicators
- Significant updates are in progress.

# Dimensions, Weights, Indicators



# Dimensions Indicators, Weights, Cutoffs

<b>Dimension (Weight)</b>	<b>Indicator (Weight)</b>	<b>Deprivation Cut-off</b>
Health (1/3)	Nutrition (1/6)	<i>Any adult or child in the household with nutritional information is undernourished<sup>1</sup></i>
	Child mortality (1/6)	<i>Any child has died in the household<sup>2</sup></i>
Education (1/3)	Years of schooling (1/6)	<i>No household member has completed five years of schooling</i>
	Child school attendance (1/6)	<i>Any school-aged child in the household is not attending school up to class 8<sup>3</sup></i>
Standard of Living (1/3)	Access to electricity (1/18)	<i>The household has no electricity</i>
	Access to improved sanitation (1/18)	<i>The household's sanitation facility is not improved or it is shared with other households</i>
	Access to safe drinking water (1/18)	<i>The household does not have access to safe drinking water or safe water is more than 30 minutes walk round trip</i>
	Type of flooring material (1/18)	<i>The household has a dirt, sand or dung floor</i>
	Type of cooking fuel (1/18)	<i>The household cooks with dung, wood or charcoal.</i>
	Asset ownership (1/18)	<i>The household does not own more than one of: radio, TV, telephone, bike, motorbike or refrigerator, and does not own a car or truck</i>

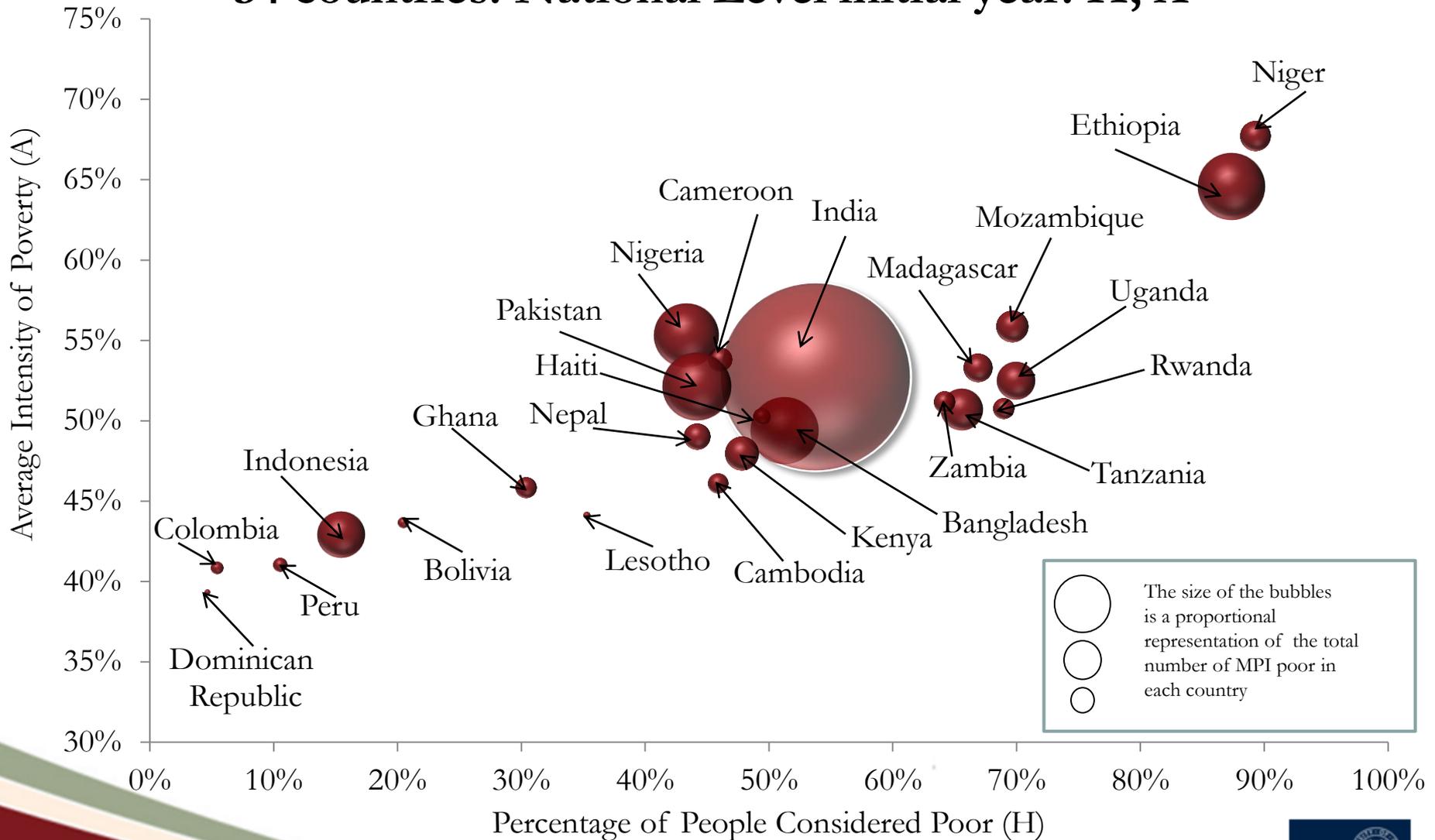
# Methodology

- Follows the global MPI, but with the comparable variables
- Uses the AF methodology with nested weights;  $k=33.33\%$
- **MPI<sub>T</sub>** are rigorously comparable
- Methodology: Chapter 9 of AFSSRB OUP 2015
  
- Standard errors, sig levels, data tables available **online**
- Implements the **destitution** measure presented next
- A linked paper focuses on measured **growth elasticities**

# Paper Structure

- Overview
- Methodological Detour: Theoretical decompositions
- Closer View: Leaving No One Behind:
  - Changes by Incidence and Intensity
  - Changes by ethnic groups & subnational regions
  - Changes by deprivation (indicator)
  - Reduction of the subset of the poor who are Destitute

# 34 countries: National Level initial year: H, A

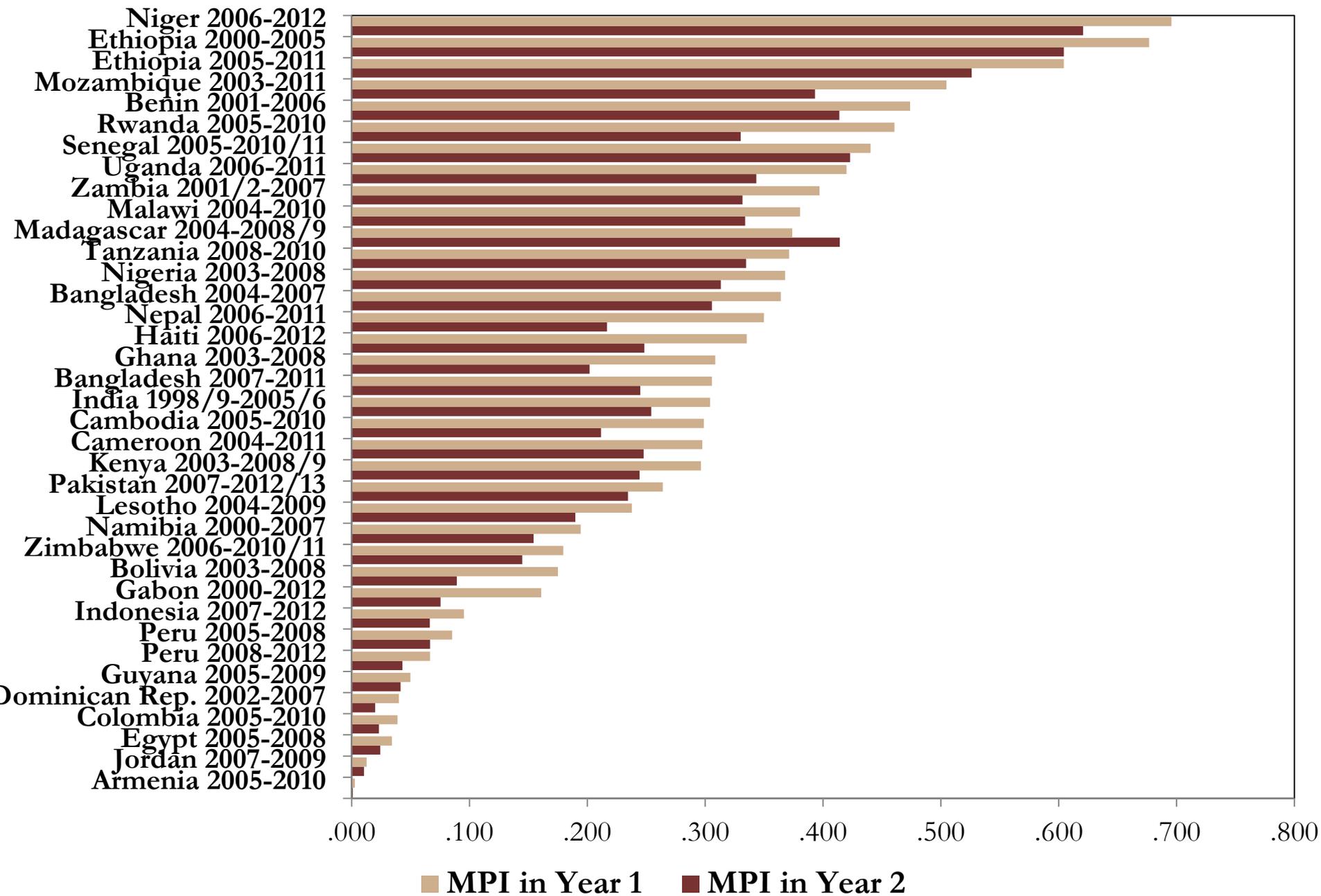


# Overview

- 30 countries (98% of covered population) have significant\* reductions in MPI by  $\alpha = 0.05$ ; 29 countries by  $\alpha = 0.01$ .
- Guyana and Peru only at  $\alpha = 0.10$
- Jordan and Senegal: no significant reductions
- Madagascar: significant increase in MPI ( $\alpha = 0.01$ )

\* significance refers to full period of comparison, not annualized changes

# MPI<sub>T</sub> over time



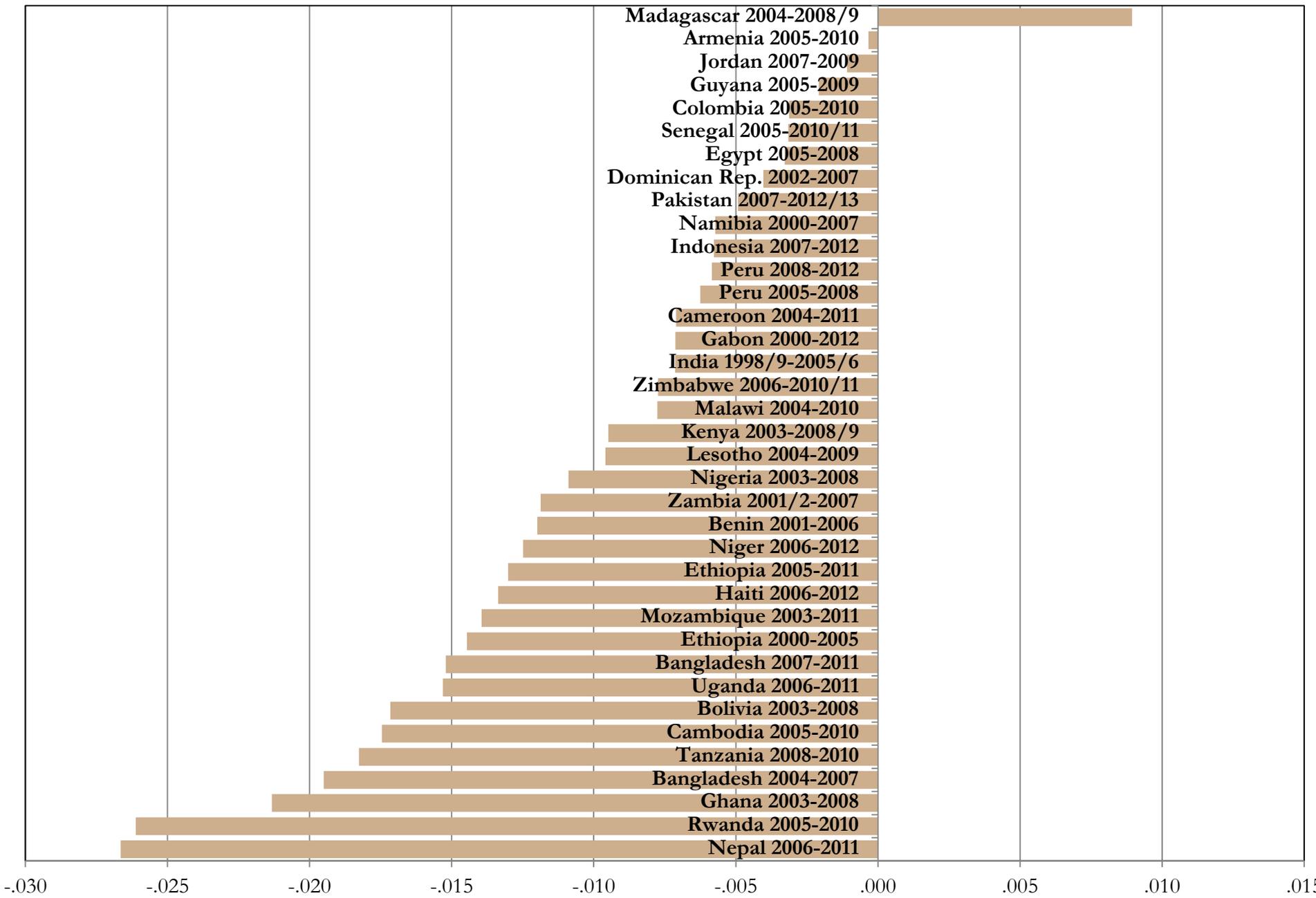
# Annualized Changes

- **Annualized Absolute Rate of Change:** is the difference in levels across two periods divided by the difference in the two time periods.

$$\bar{\Delta}M_0 = \frac{M_0(X_{t^2}) - M_0(X_{t^1})}{t^2 - t^1}$$

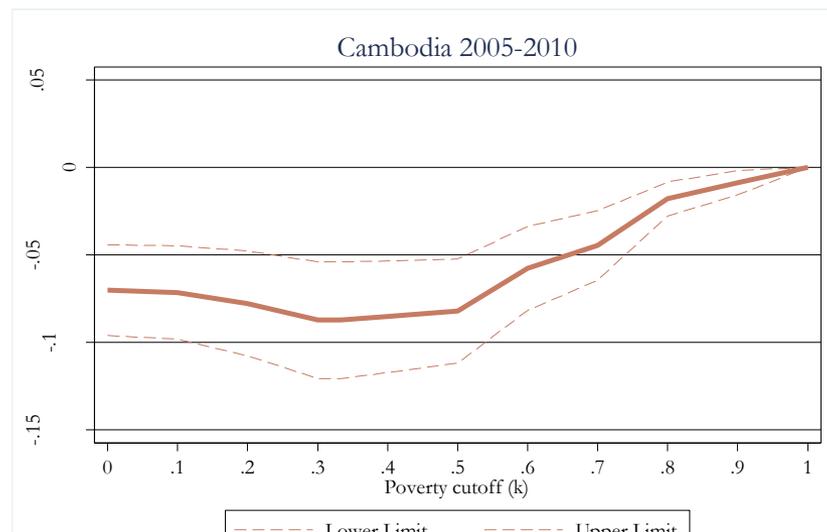
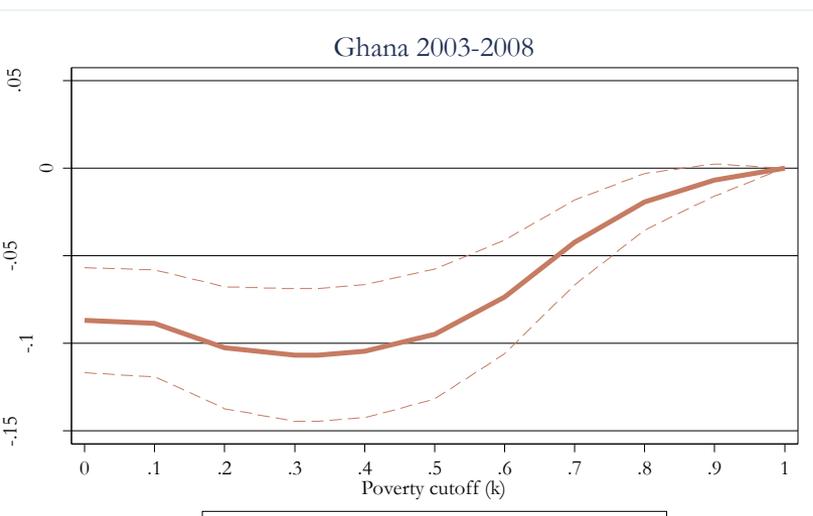
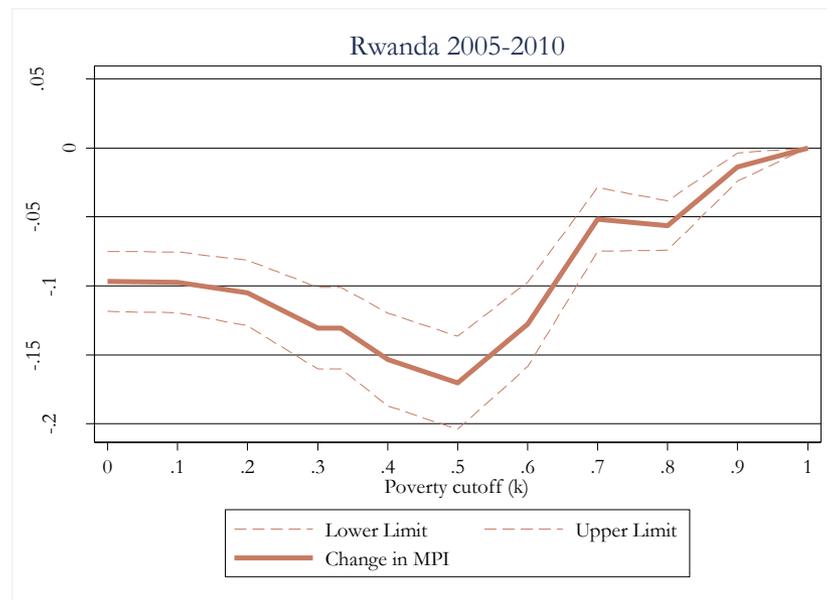
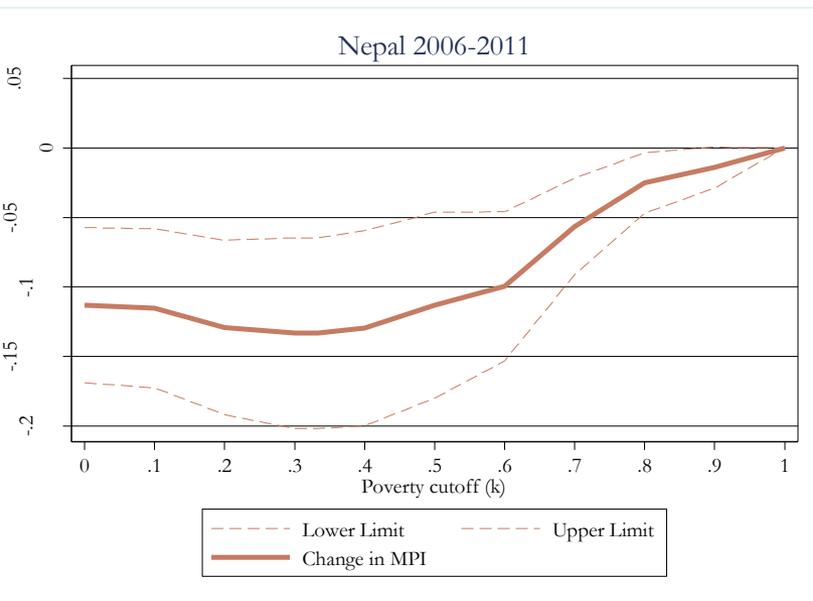
- **Relative Rate of Change:** is the compound rate of reduction per year between the initial and the final periods.

$$\bar{\delta}M_0 = \left[ \left( \frac{M_0(X_{t^2})}{M_0(X_{t^1})} \right)^{\frac{1}{t^2 - t^1}} - 1 \right] \times 100$$



■ Annualized Absolute Change in MPI

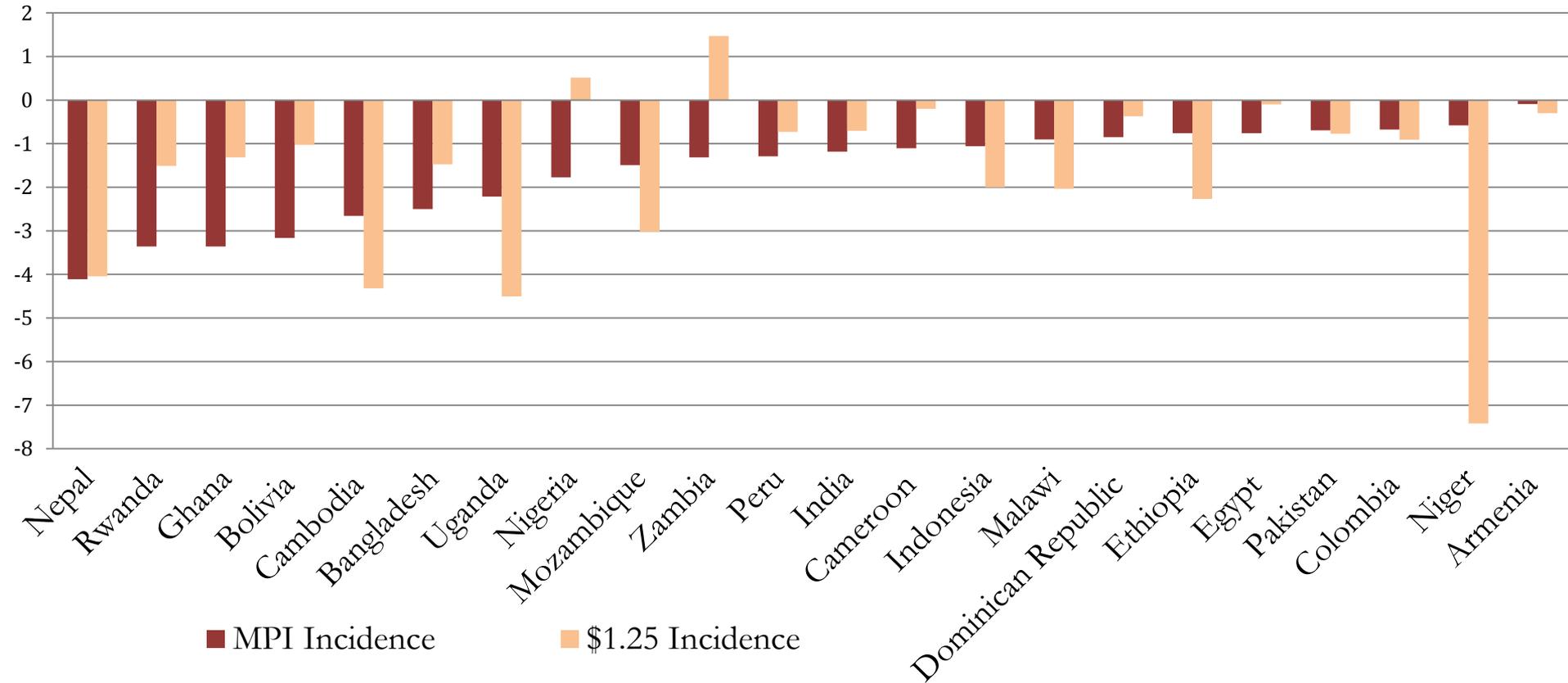
# Note: robustness tests online (e.g. for $k$ )



# MPI (H) and \$1.25/day Income poverty (H)

- Matching years available for 7 countries (Armenia, Colombia, Dominican Republic, Egypt, Ethiopia, Malawi: in 4 of these rate of \$1.25/day reduction exceeds MPI reduction)
- Linear interpolation or extrapolation used for \$1.25/day for 18 countries
- Total of 22 comparisons that reduced MPI (H) significantly.
- Initial levels of MPI (H) exceeded income poverty (H) in 19 of 25 countries.
- Reduction patterns are not identical, so require further study.

# MPI (H) and \$1.25/day Income poverty (H)



Tabita, Kenya

Rabiya, India

Stephanie, Madagascar

Agathe, Madagascar

Dalima, Kenya

Ann-Sophie, Kenya

Valerie, Madagascar



# Methodological Interlude:

Dynamic Subgroups Analysis using  
repeated Cross-Sectional data

# Dynamic Subgroups – Repeated Cross-Section Data

- It is impossible to decompose  $\Delta M_0$  with the empirical precision as when using panel data
- However we do care about the extent to which the **poorest of the poor** reduced the **intensity** of their poverty or **exited** poverty.
- Consider 2 groups:

***Movers:*** those who changed status across periods ( $\Delta H$ )

***Stayers:*** ongoing poor plus the proportion of previously poor people who were replaced by ‘new poor’ ( $H(X_{t2})$ )

# Change in $M_0$

- If poverty reduced and the group of people who entered poverty is empirically small (assumptions)
- Change in  $M_0$  can be decomposed as follows:

$$\Delta M_0 = \underbrace{\Delta H \times A^{\hat{E}}}_{\text{Movers Effect}} + \underbrace{H(X_{t^2}) \times \Delta A^{\hat{O}}}_{\text{Stayers Effect}}$$

How to obtain  $A^{\hat{E}}$  and  $A^{\hat{O}}$ ?

# Apablaza and Yalonetzky

Assumptions:

- $A^{\hat{E}}$  is assumed to be the **average intensity** in period 2.
- $\Delta A^{\hat{O}}$  is assumed to equal the **simple difference in intensities** of the poor across the two periods

$A^{t^1}$	Exclusive intensity effect	Joint effect	$M_0^{t^1}$
$A^{t^2}$		Exclusive incidence effect	$M_0^{t^2}$
			$H^{t^2}$ $H^{t^1}$

# Apablaza and Yalonetzky

$$\Delta M_0 = A^{t^2} \Delta H + H^{t^2} \Delta A + (H^{t^2} - H^{t^1})(A^{t^2} - A^{t^1})$$

Effect from  
entry and exit

Effect among  
ongoing poor

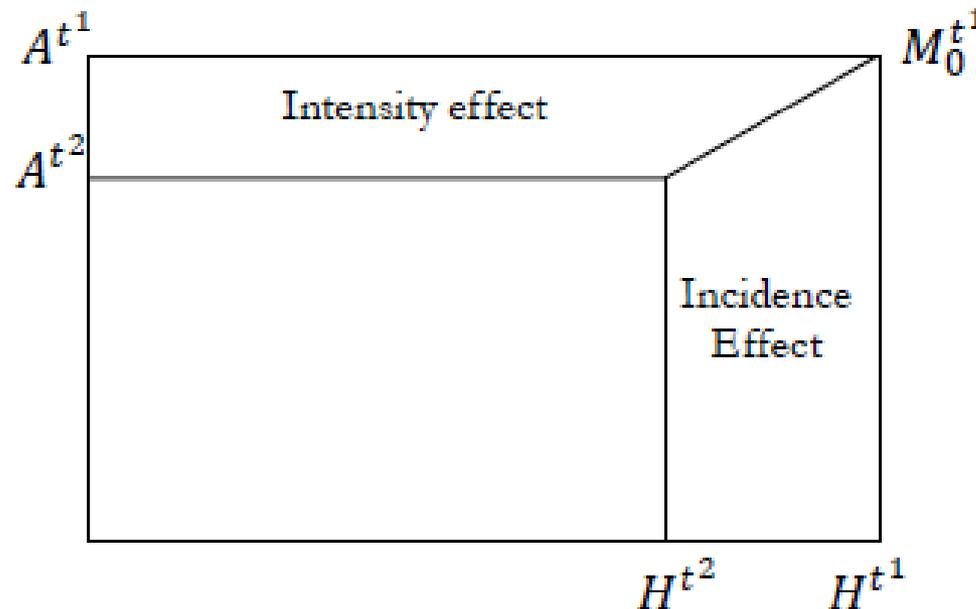
Interaction  
effect

$A^{t^1}$	Exclusive intensity effect	Joint effect	$M_0^{t^1}$
$A^{t^2}$		Exclusive incidence effect	
			$M_0^{t^2}$
			$H^{t^2}$ $H^{t^1}$

# Roche – Shapley Decomposition

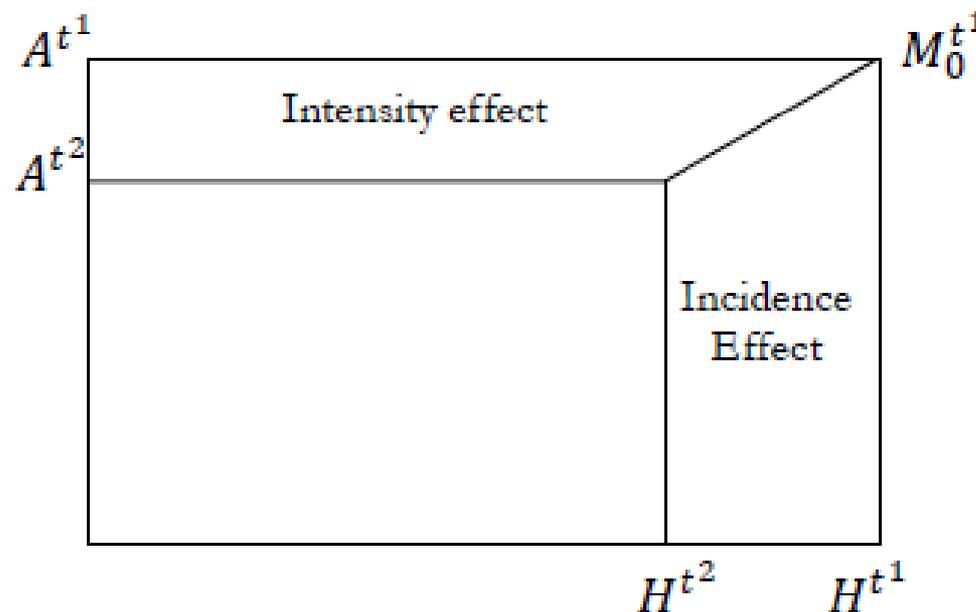
Assumptions:

- $A^{\hat{E}}$  is assumed to be the **average intensity** for the two periods.
- The percentage of ongoing poor is assumed to be the **average incidence** for the two periods



# Roche – Shapley Decomposition

$$\Delta M_0 = \underbrace{\frac{A^{t^2} + A^{t^1}}{2} \Delta H}_{\text{Incidence effect}} + \underbrace{\frac{H^{t^2} + H^{t^1}}{2} \Delta A}_{\text{Intensity effect}}$$



# Upper and Lower Estimates - empirical

Estimate lower and upper bound estimates for  $A^{\hat{E}}$ ,  $\Delta A^{\hat{O}}$

If less poor people moved out of poverty

- Identify the  $\Delta H \times n$  poor persons having the lowest intensity
- Use the average of those scores for  $A^{\hat{E}}$  then solve for  $A^{\hat{O}}$

If poorest people moved out of poverty

- Identify the  $\Delta H \times n$  poor persons having the highest intensity
- Use the average of those scores for  $A^{\hat{E}}$  then solve for  $A^{\hat{O}}$

# Example

Country	Upper Bound				Lower Bound			
	A Movers	$\Delta A$ Stayers	Movers Effect	Stayers Effect	A Movers	$\Delta A$ Stayers	Movers Effect	Stayers Effect
Ethiopia 2005-2011	0.99	-0.03	68.7%	31.3%	0.38	-0.07	26.6%	73.4%
Nepal 2006-2011	0.74	0.04	113.4%	-13.4%	0.38	-0.13	58.2%	41.8%
Peru 2005-2008	0.59	0.02	119.5%	-19.5%	0.33	-0.04	67.1%	32.9%
Rwanda 2005-2010	0.78	0	101.4%	-1.4%	0.36	-0.1	47.1%	52.9%
Senegal 2005-2010/11	1	-0.02	26.8%	73.2%	0.33	-0.02	8.9%	91.1%

- The upper and lower bounds are wide apart and vary across countries.
- The real contributions could vary within this range.
- Can we guess which effect had the biggest contribution? Not necessarily (Ethiopia, Rwanda)

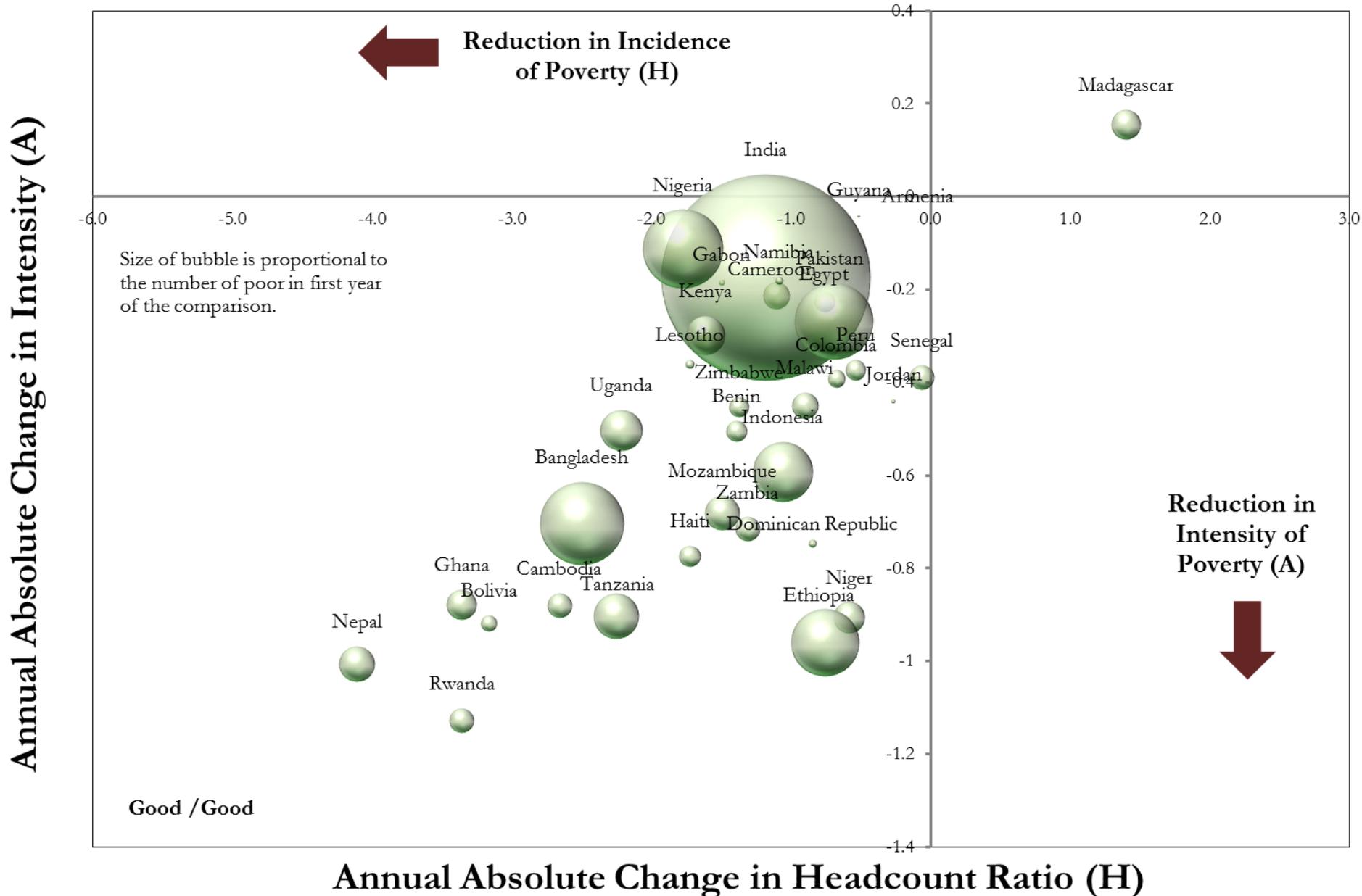
# Example: Shapley

Country	Upper Bound				Lower Bound				Decomposition	
	A Movers	$\Delta A$ Stayers	Movers Effect	Stayers Effect	A Movers	$\Delta A$ Stayers	Movers Effect	Stayers Effect	Incidence Effect H	Intensity Effect A
Ethiopia 2005-2011	0.99	-0.03	68.7%	31.3%	0.38	-0.07	26.6%	73.4%	45%	55%
Nepal 2006-2011	0.74	0.04	113.4%	-13.4%	0.38	-0.13	58.2%	41.8%	79%	21%
Peru 2005-2008	0.59	0.02	119.5%	-19.5%	0.33	-0.04	67.1%	32.9%	86%	14%
Rwanda 2005-2010	0.78	0	101.4%	-1.4%	0.36	-0.1	47.1%	52.9%	68%	32%
Senegal 2005-2010/11	1	-0.02	26.8%	73.2%	0.33	-0.02	8.9%	91.1%	16%	84%

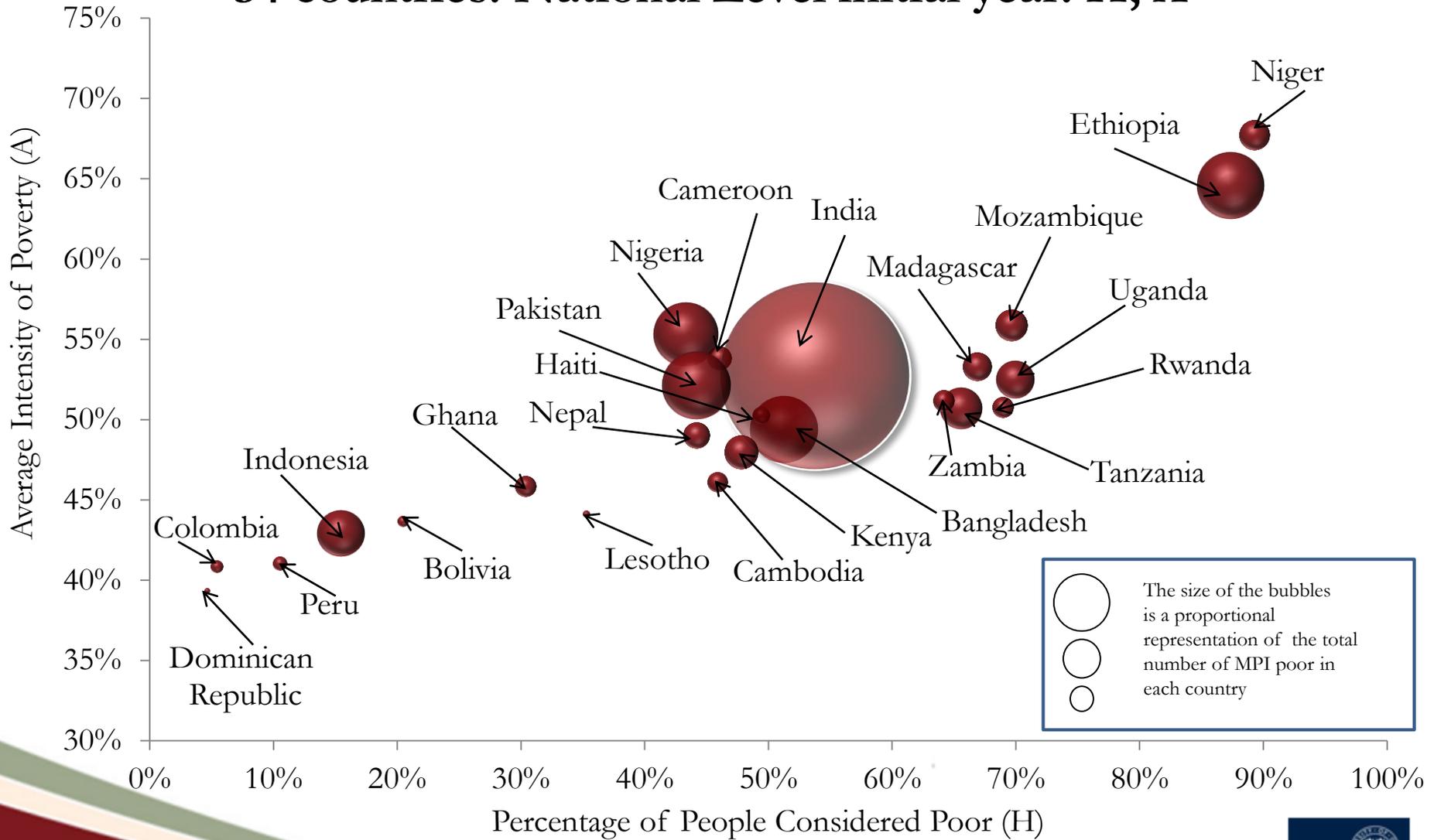
- Shapley decomposition lies between the upper and lower bounds.
- Shapley decomposition has the appeal of appearing to provide point estimates.
- But the underlying assumptions are strong and not validated.

**It may be better to be ‘vaguely right than precisely wrong’.**

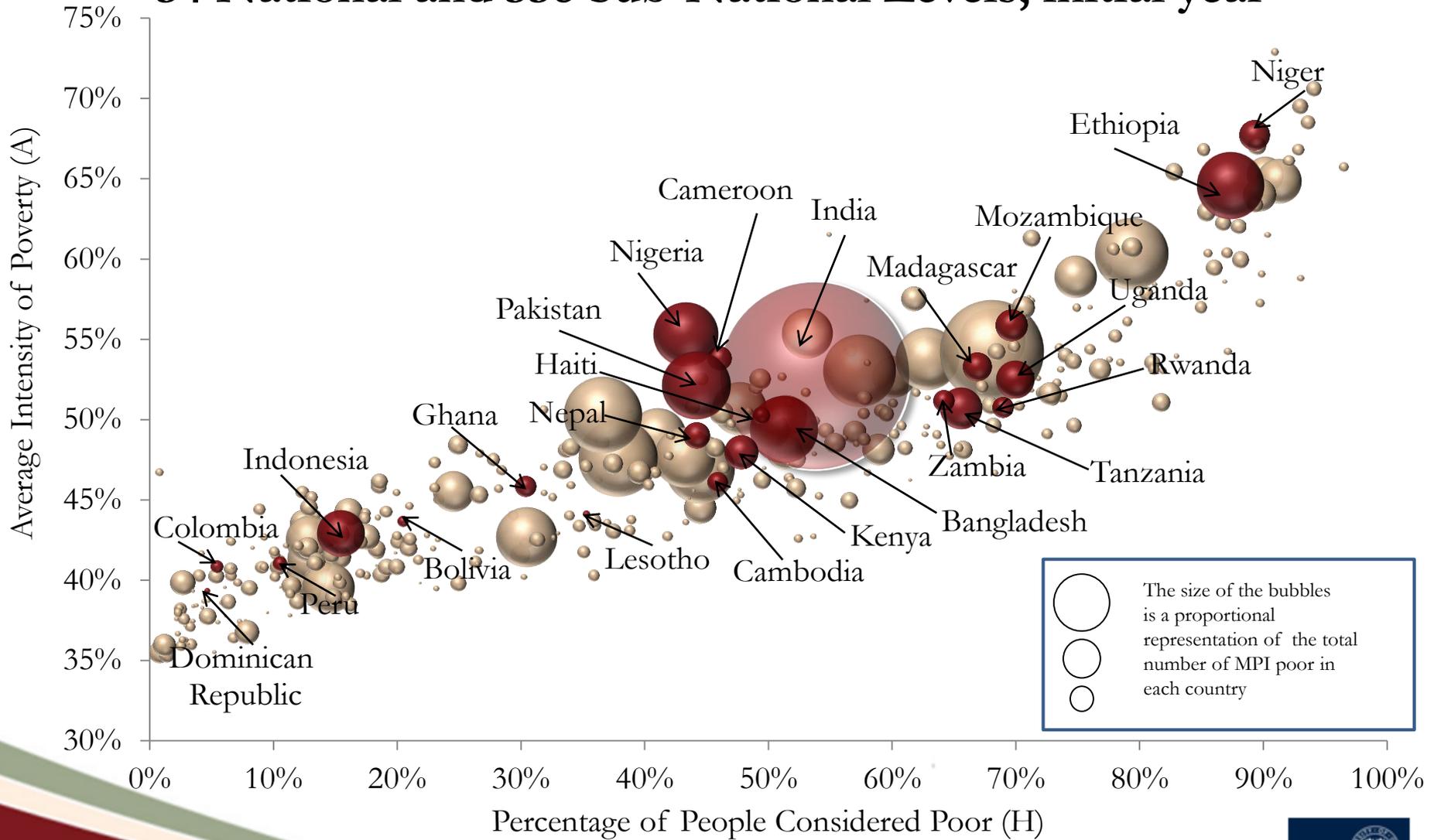
# Reductions in Headcount ratio H and Intensity A



# 34 countries: National Level initial year: H, A

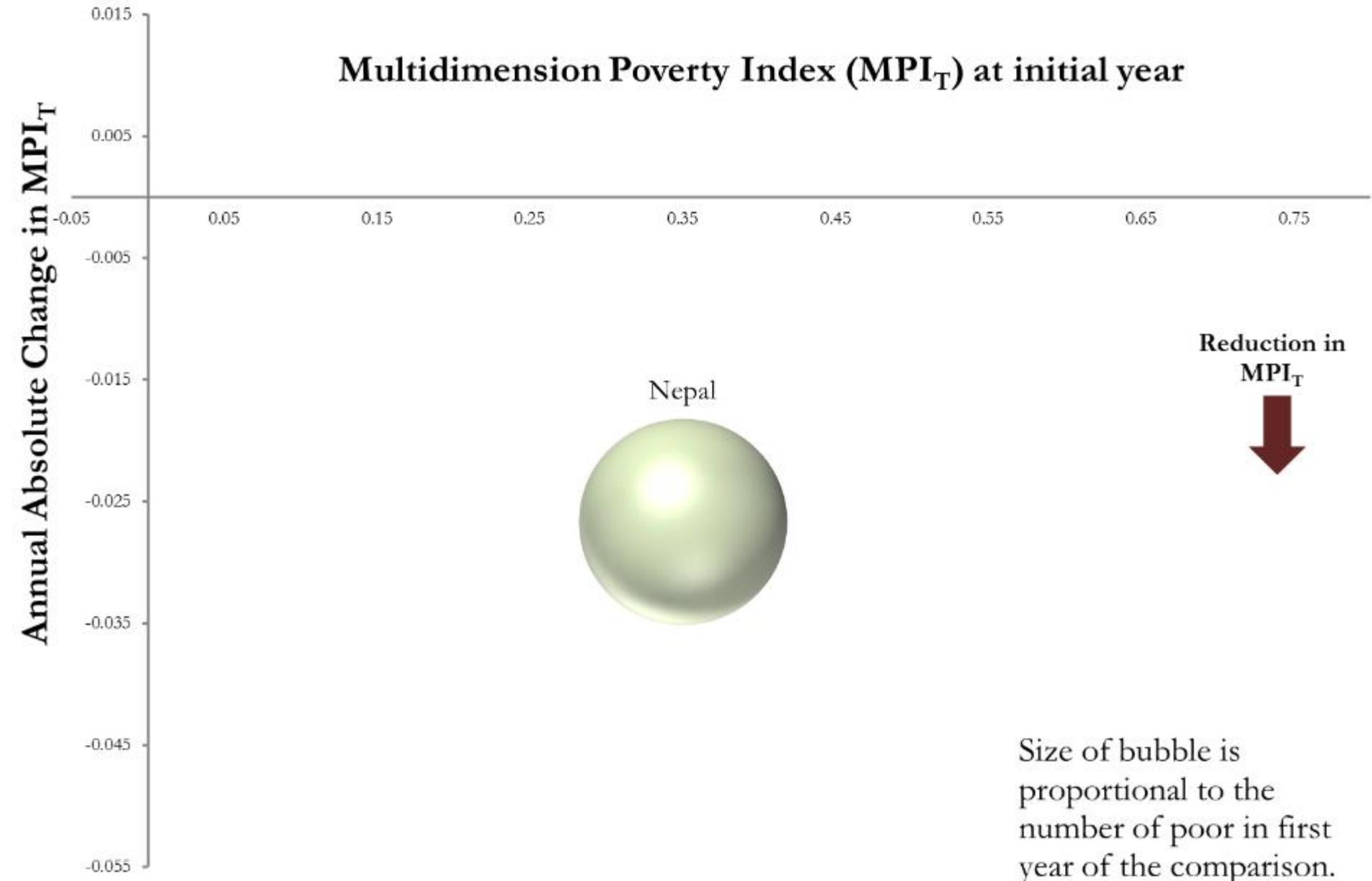


# 34 National and 338 Sub-National Levels, initial year



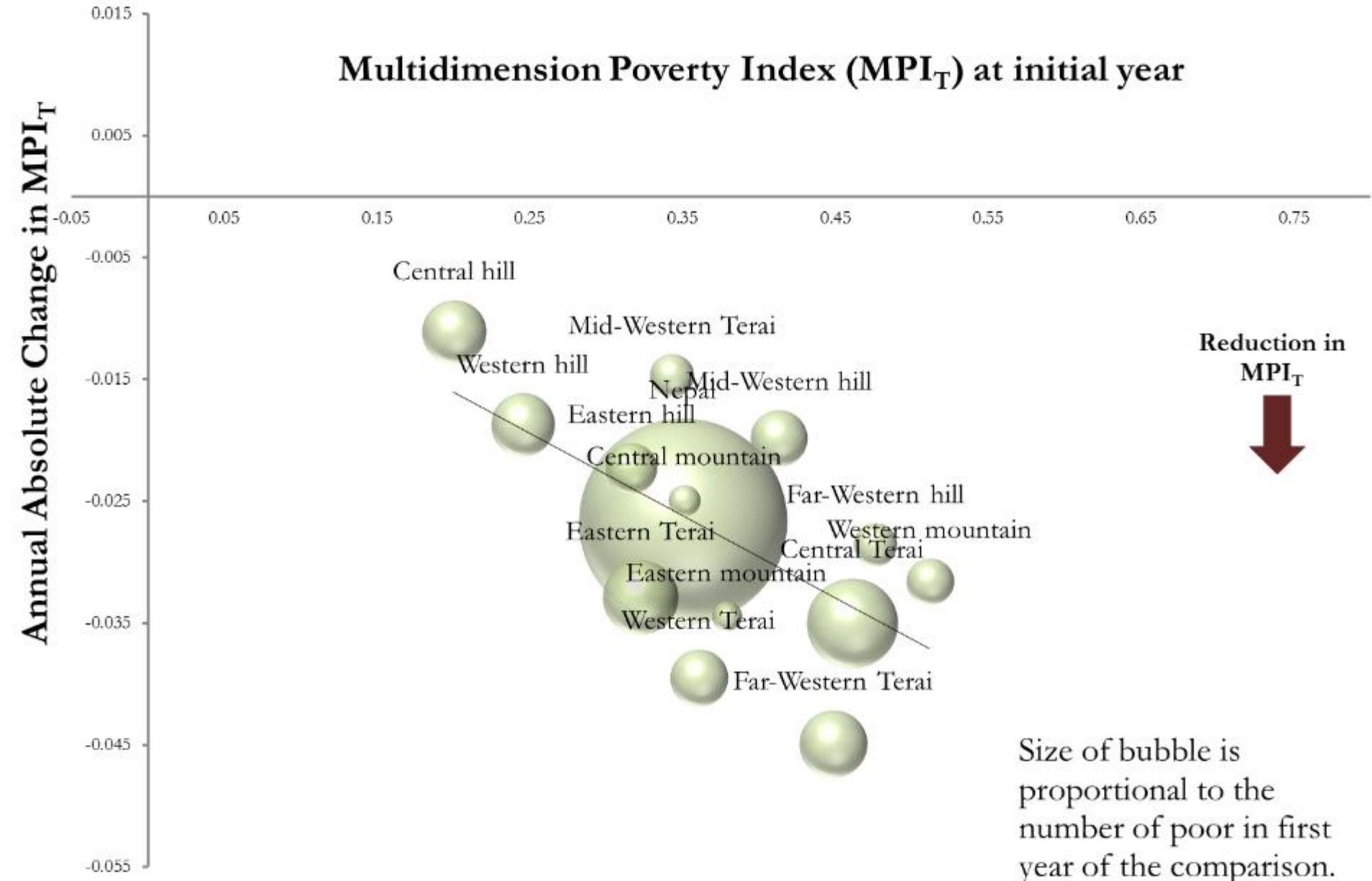
The size of the bubbles is a proportional representation of the total number of MPI poor in each country

# Subgroup Decompositions

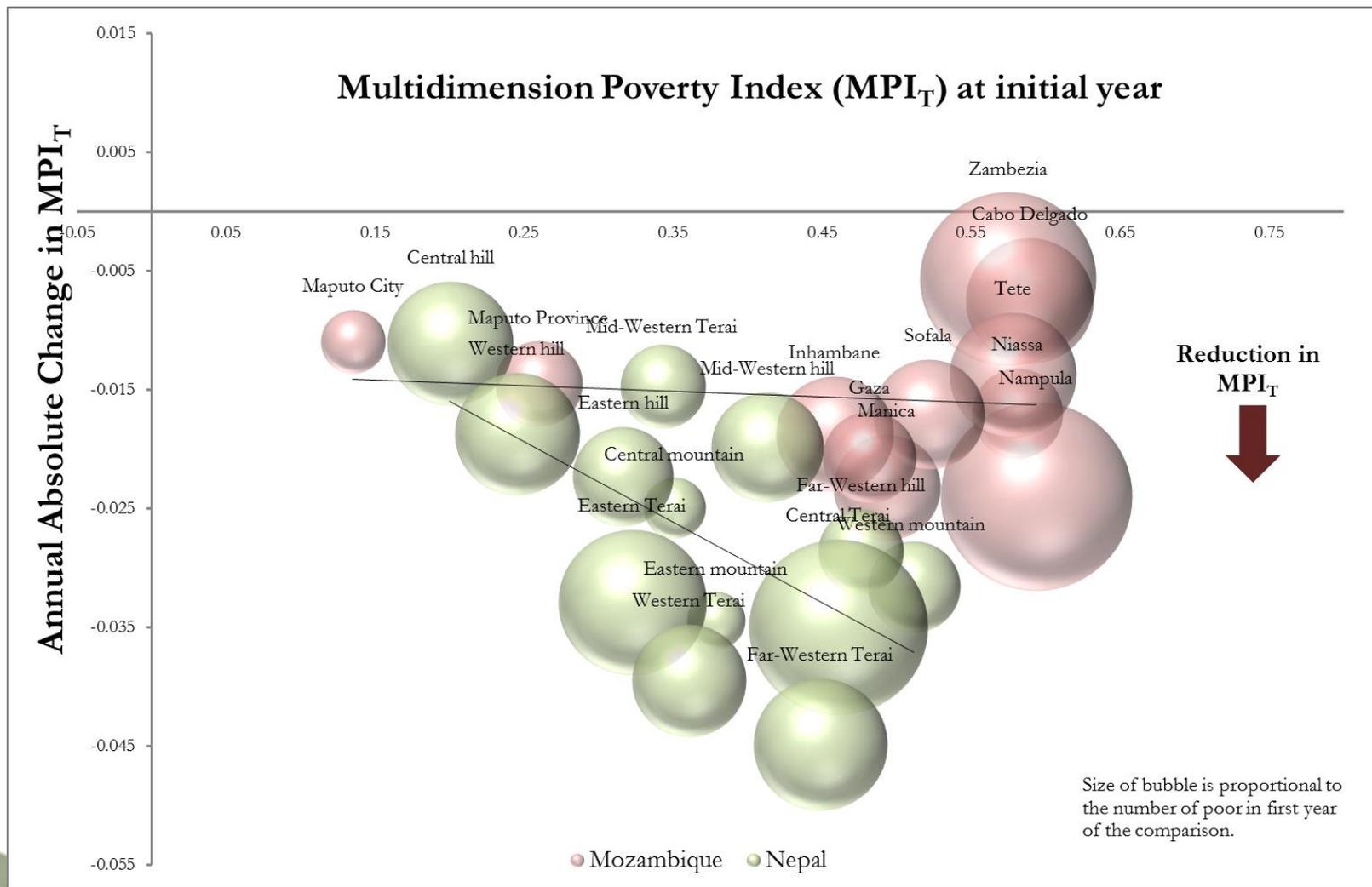


# Subgroup Decompositions

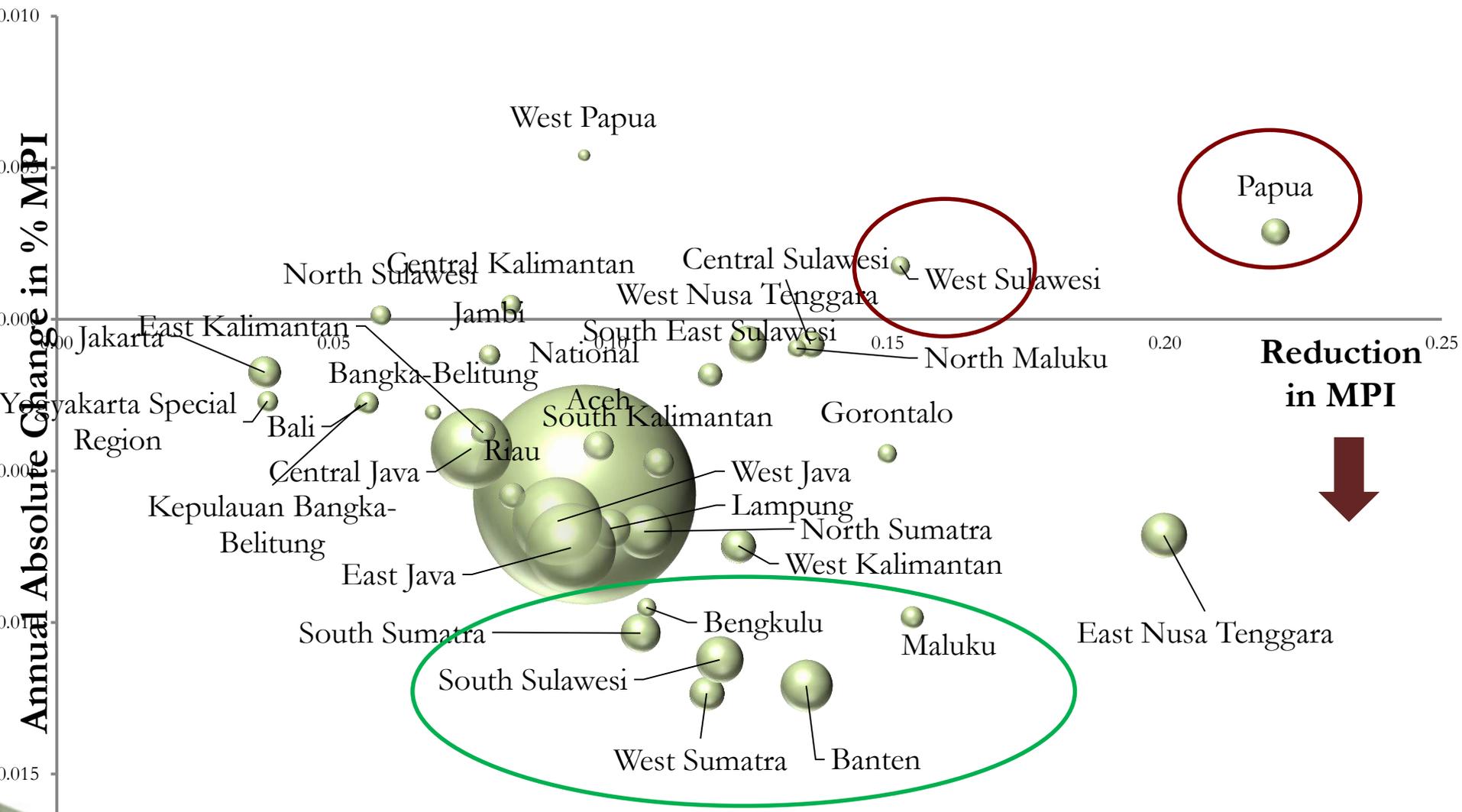
Multidimension Poverty Index ( $MPI_T$ ) at initial year



# Poverty reduction in regions of Mozambique and Nepal



# Indonesia MPI Reduction 2007-12 by subnational regions

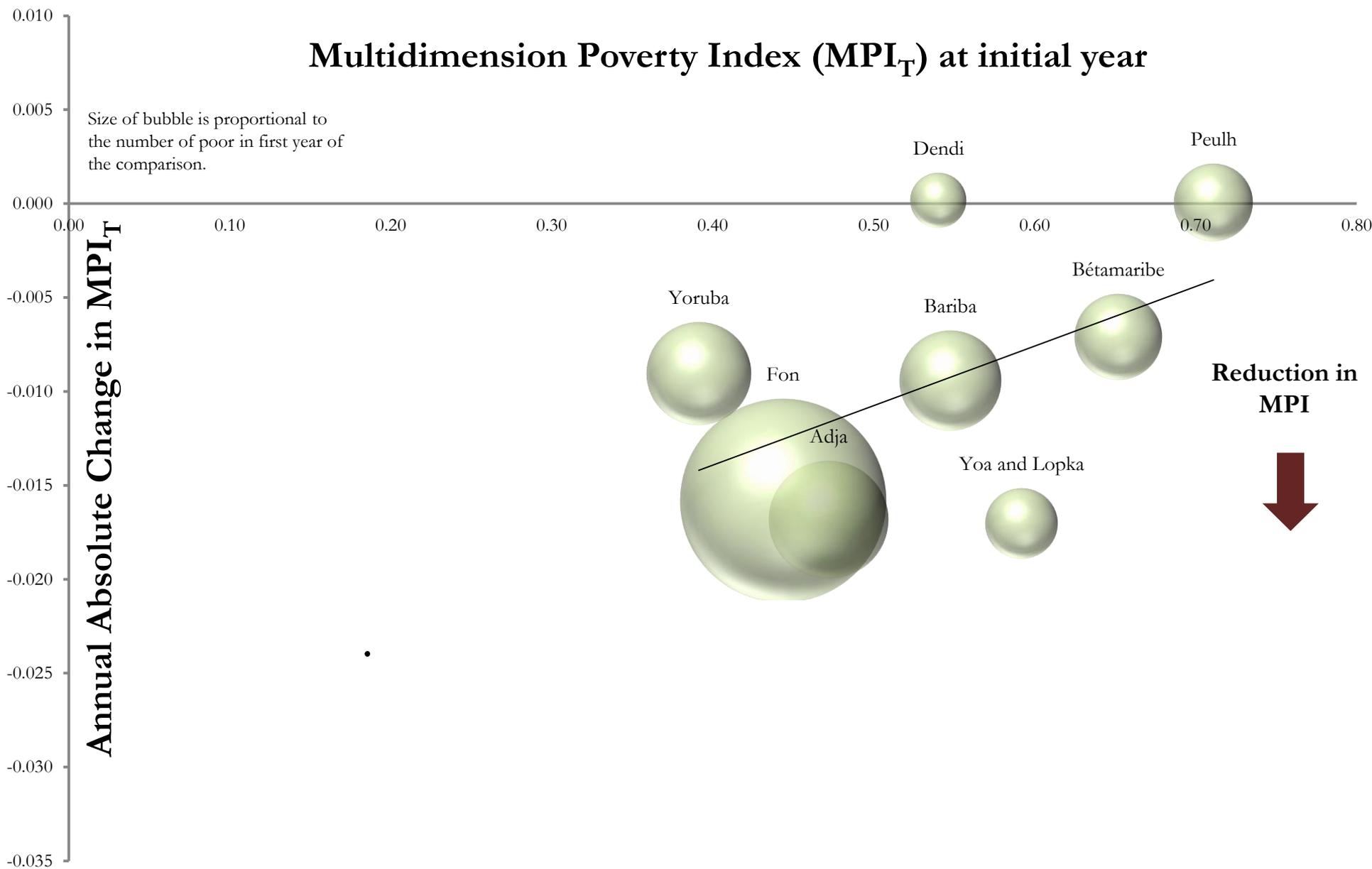


Multidimensional Poverty Index (MPI) at initial year

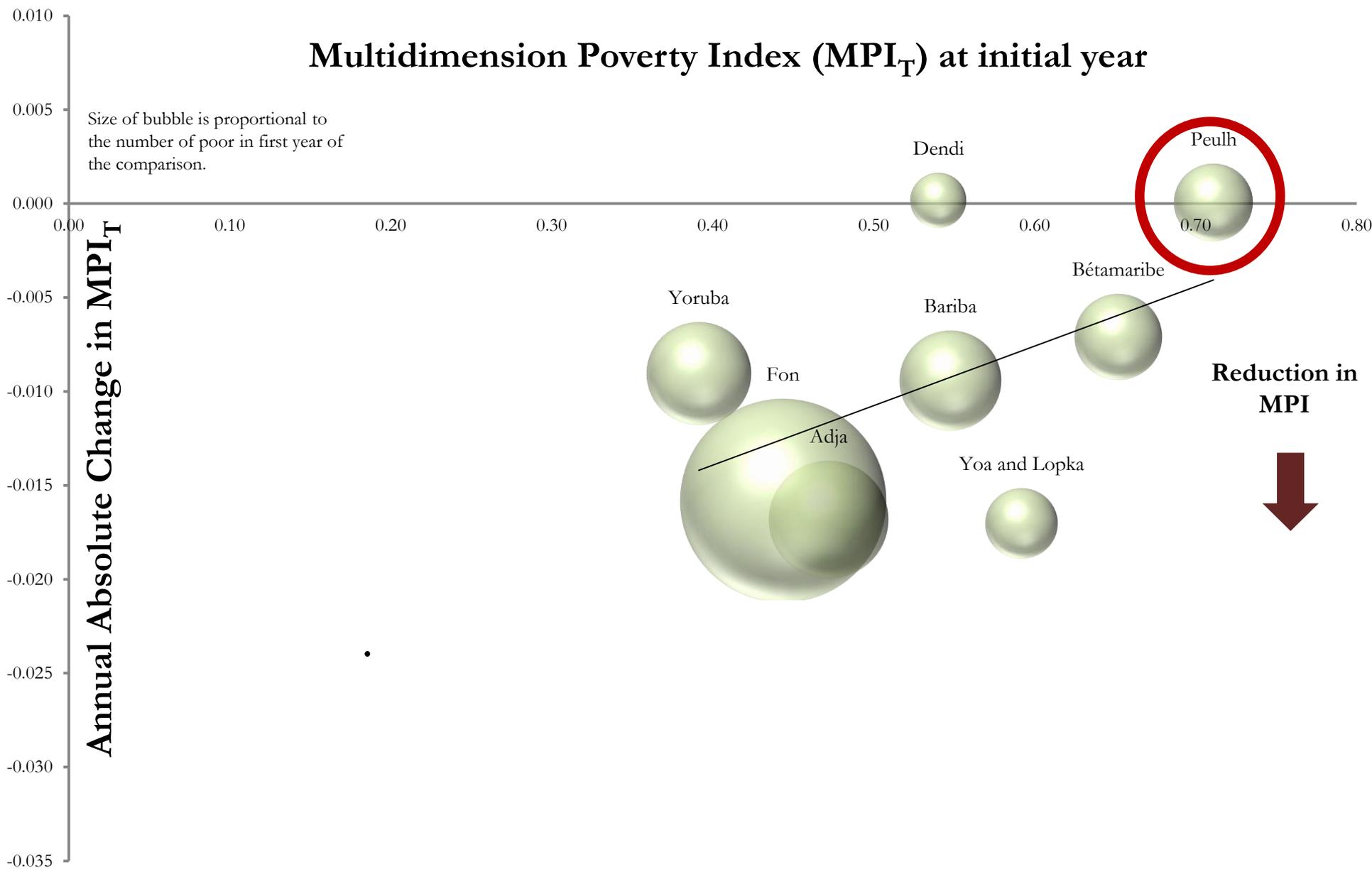
# Disaggregation by subnational regions: Summary results

- A total of 208 regions, representing 78% of our sample, showed **statistically significant** reduction in MPI.
- Eight countries: Bangladesh 2007-11, Bolivia, Gabon, Ghana, Malawi, Mozambique, Niger and Rwanda – had significant reductions in **each subnational region**.
- In nine countries the **poorest region** had the fastest reduction (Bangladesh 2007-11, Bolivia, Colombia, Egypt, Kenya, Malawi, Mozambique, Namibia, Niger)
- Subnational **disparities increased** in Ethiopia (2000-5), Indonesia, Jordan, Mozambique, Niger, Nigeria, Pakistan, Tanzania and Zambia.

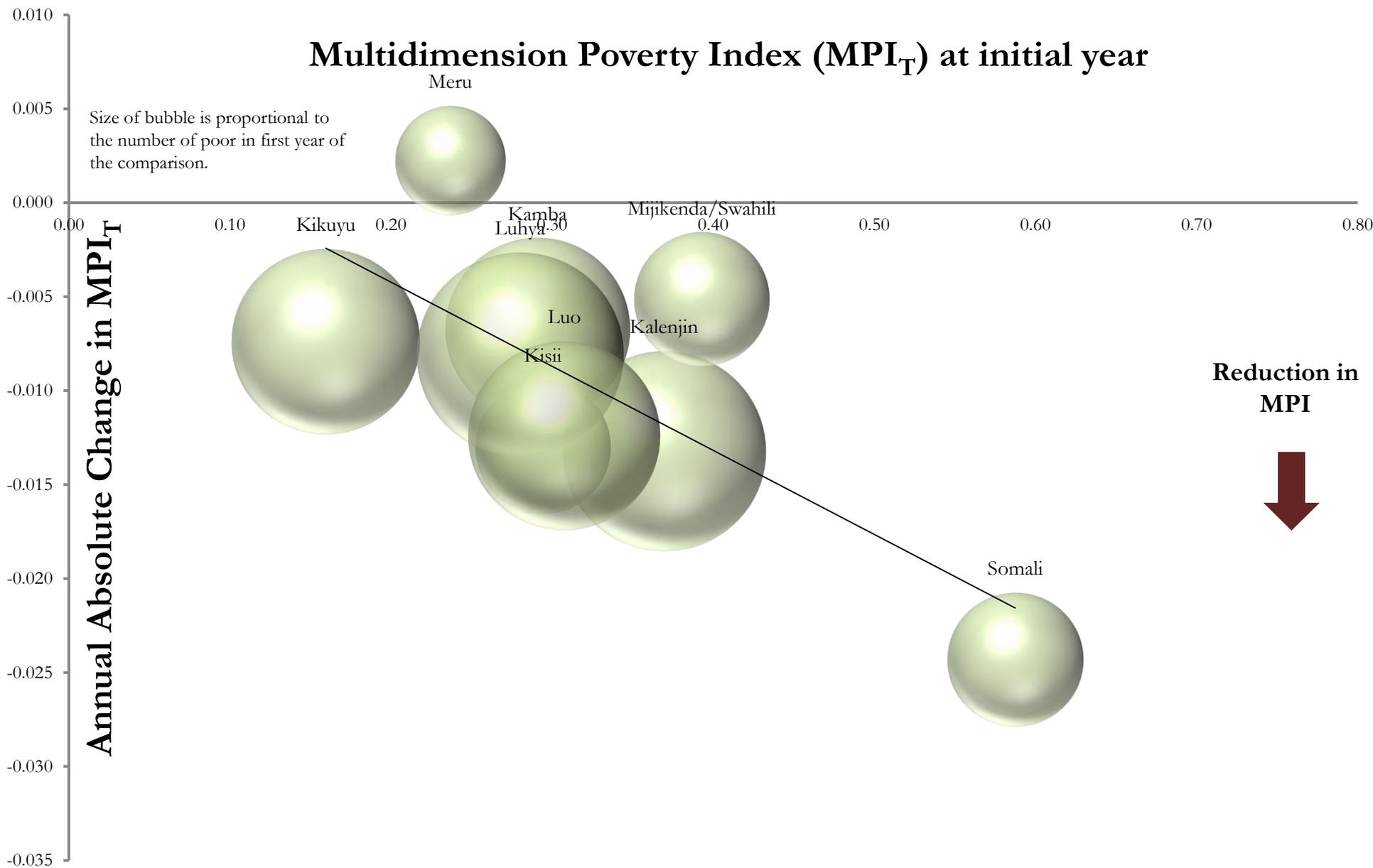
# Disaggregating by ethnic group - Benin



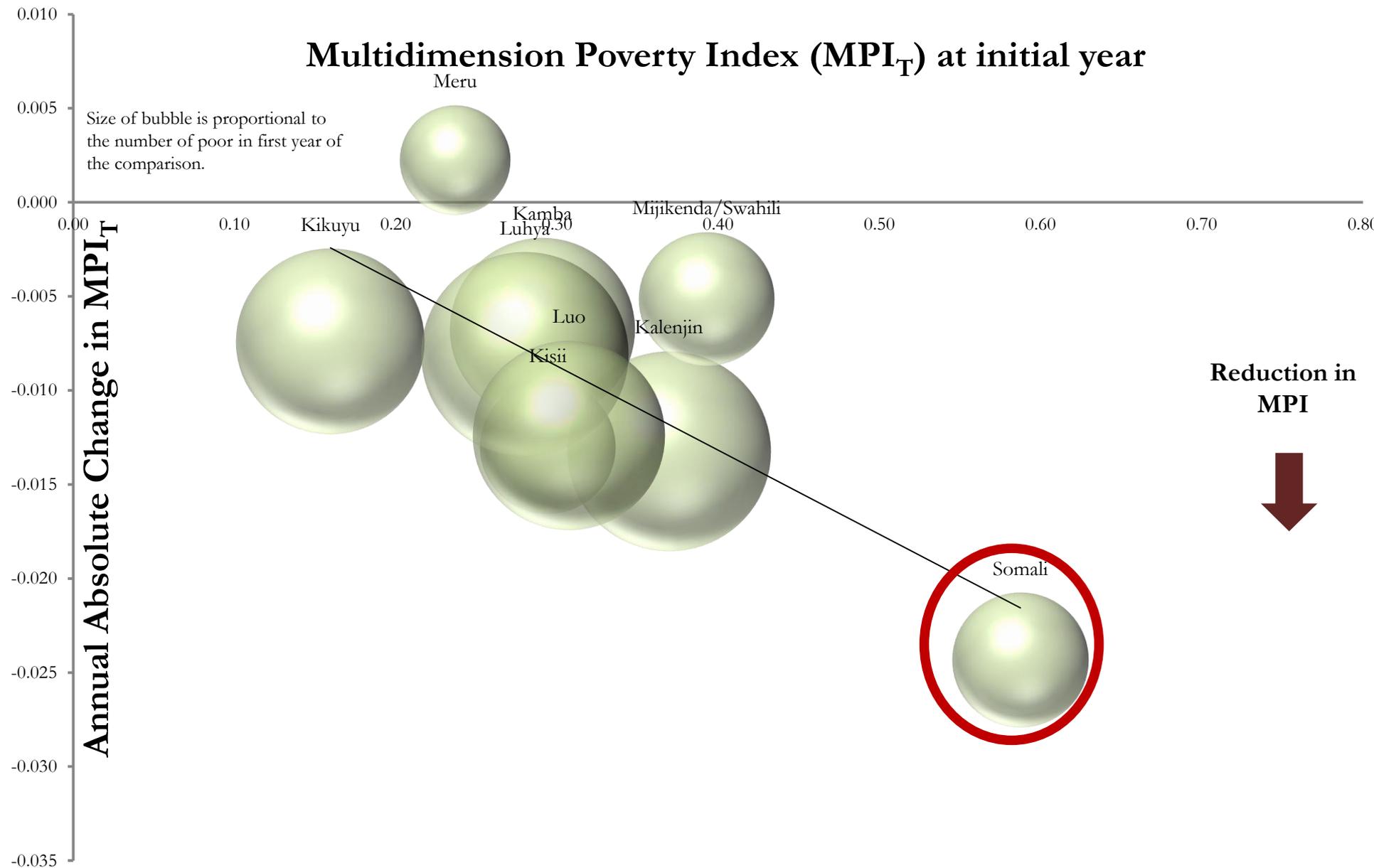
# Disaggregating by ethnic group - Benin



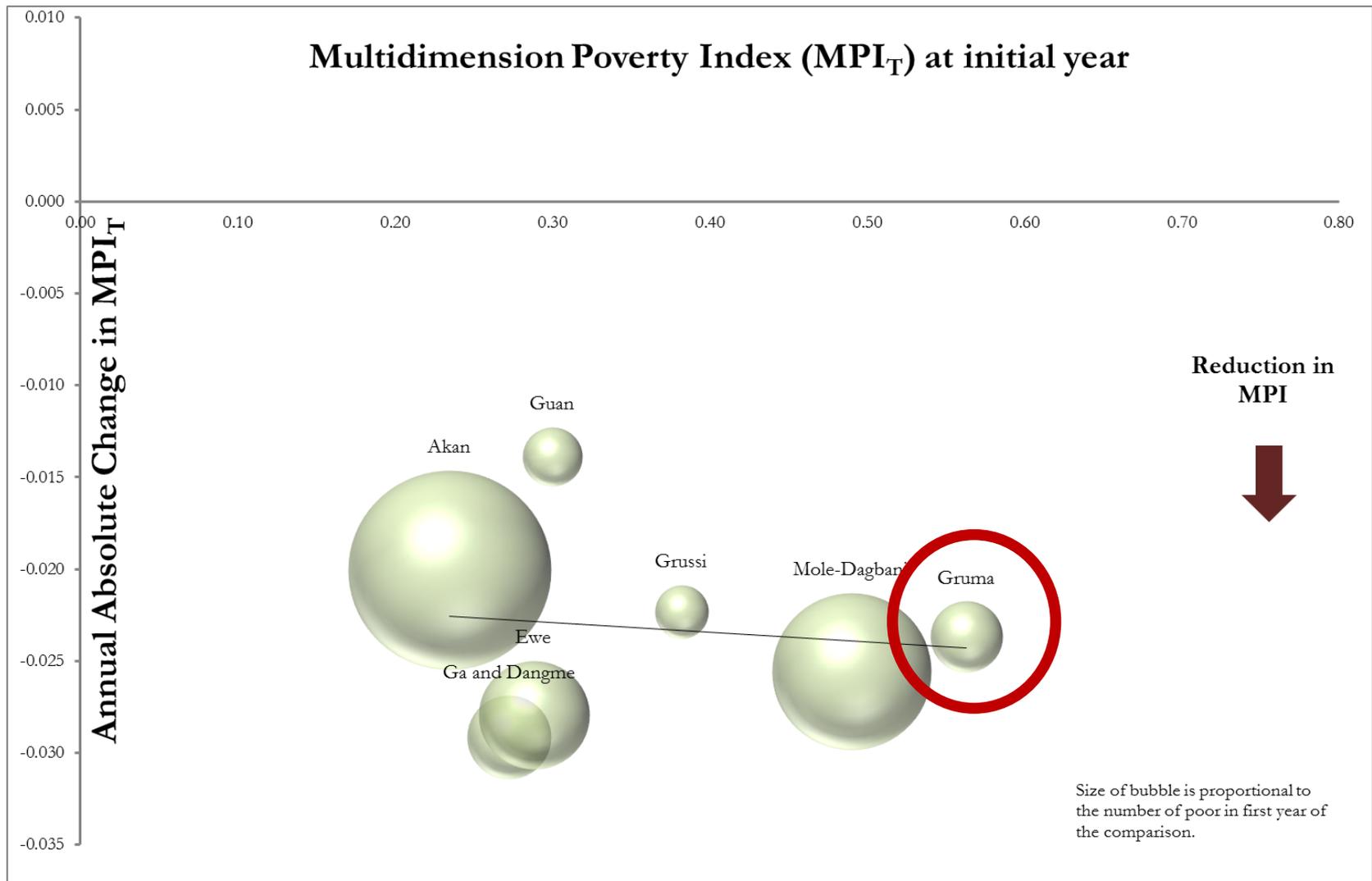
# Disaggregating by ethnic group - Kenya



# Disaggregating by ethnic group - Kenya



# Disaggregating by ethnic group - Ghana



# Dimensional Changes

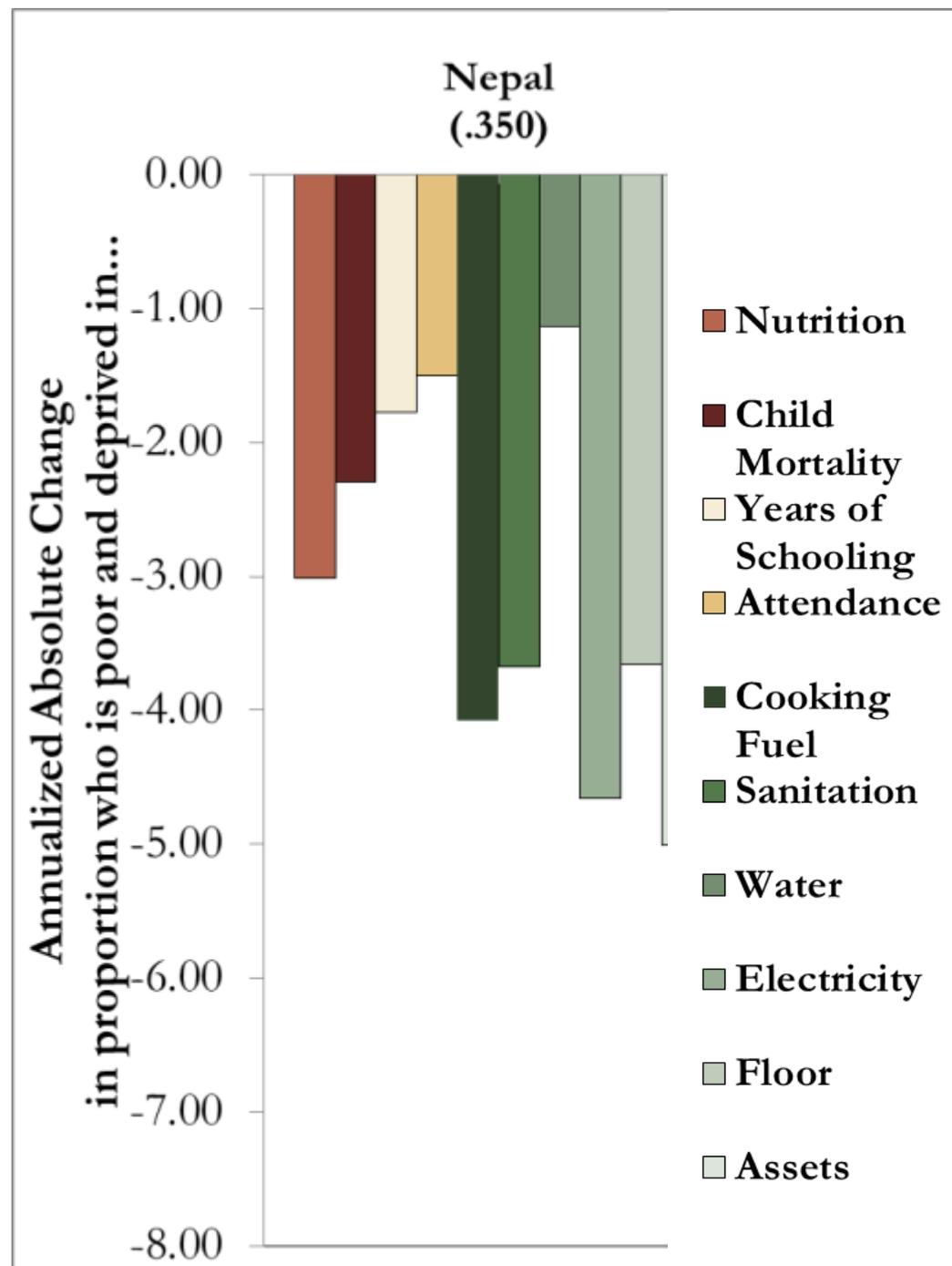
- The (annualized) absolute rate of change in  $M_0$  can be expressed as the weighted  $w_j$  average of the (annualized) absolute rates of change in censored headcount ratios  $h_j$ .

$$\bar{\Delta}M_0 = \sum_{j=1}^d w_j \bar{\Delta}h_j(k)$$

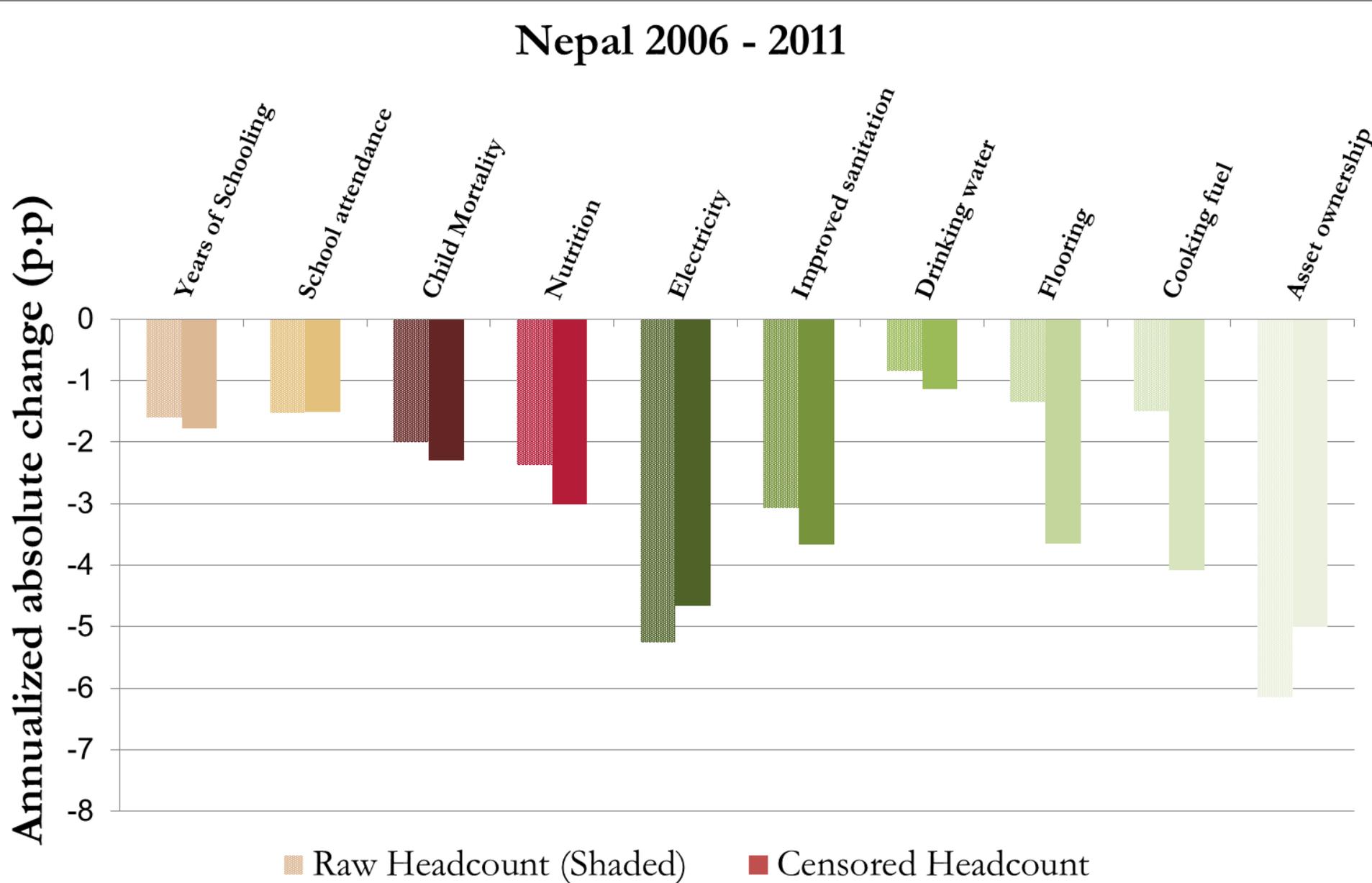
- When different indicators have different weights, the effects of their changes on the change in  $M_0$  reflect these weights.

## Change in censored headcount ratios

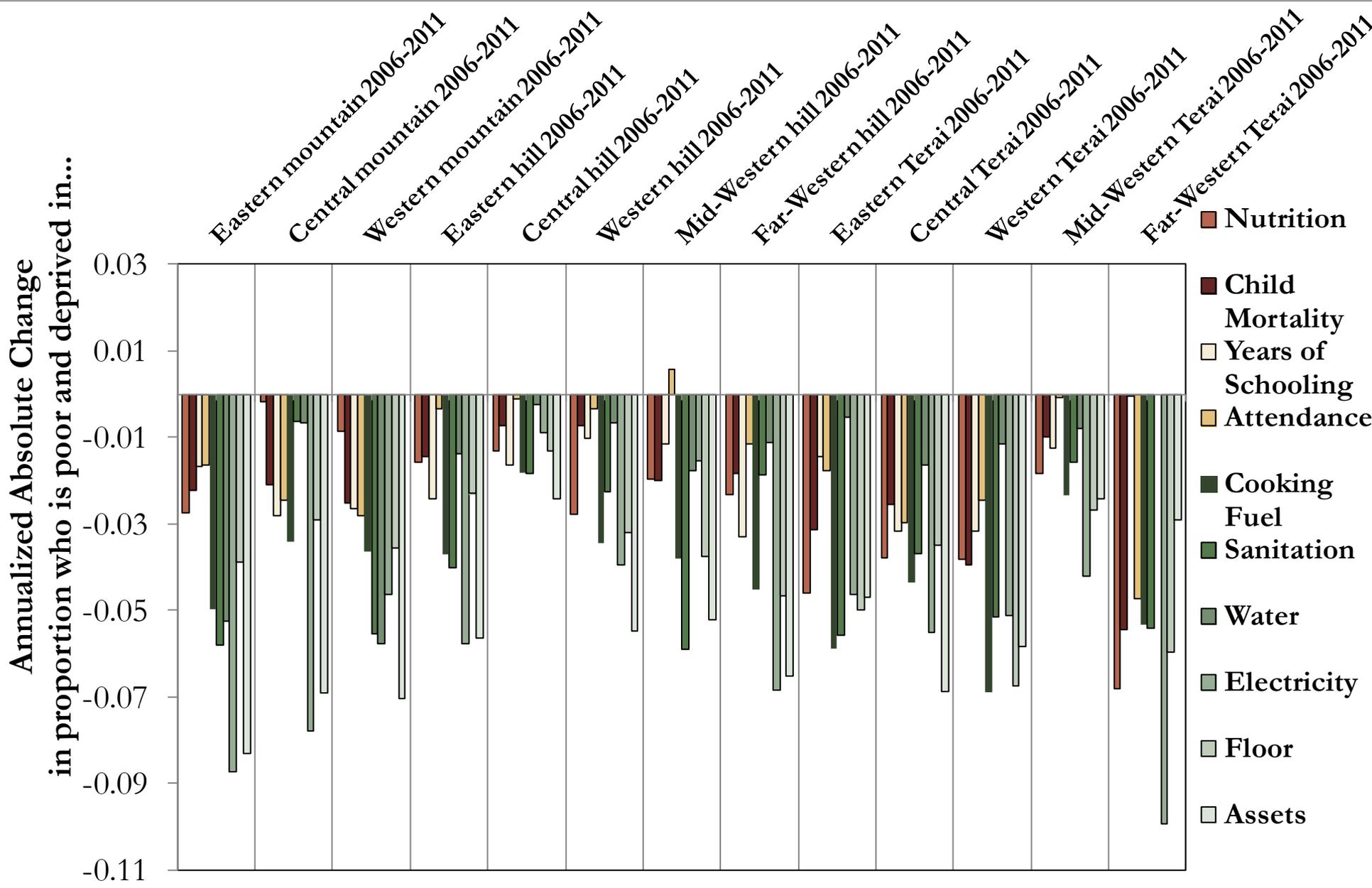
- If a deprivation is reduced
- If a person deprived in that indicator becomes non-poor



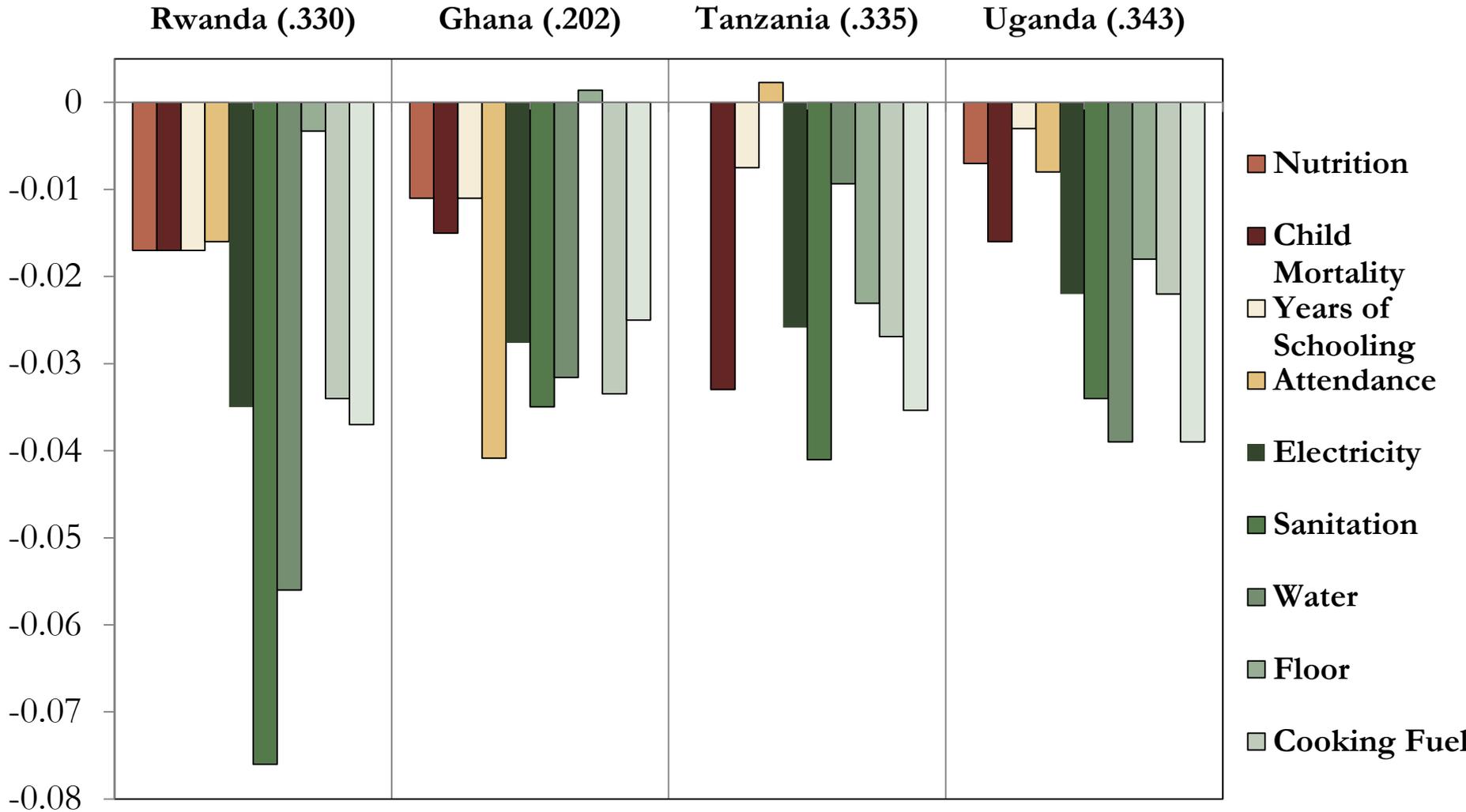
# Changed in Censored and Uncensored $h_j$



# Indicator Changes by region (Nepal)



# Changes in censored headcount ratios



# Changes in Indicators: Summary results

- Ten countries had significant reductions in **each indicator** (censored headcount ratios): Bolivia, Cambodia, Colombia, the Dominican Republic, Gabon, India, Indonesia, Mozambique, Nepal, and Rwanda.
- Each of the 10 component indicators had the **fastest** reduction in some region.
- Overall, the fastest absolute reduction on average was access to sanitation.

# Destitute: A Subset of the Poor

We implement destitution measures across each of these 34 countries and study their dynamics

- **Indicators:** Same as MPI
- **Weights:** Same as MPI
- **Poverty cutoff:** Same as MPI
- **Deprivation cutoffs:** **Deeper**

*All destitute people are also MPI poor.*

Alkire, Conconi and Seth 2014

# Deprivation cutoffs: Destitute

Indicator	Destitution Cutoff
Schooling 1/6	<b>No one has completed more than one year of schooling</b>
Attendance 1/6	<b>All primary school aged children are out of school</b>
Nutrition 1/6	<b>Someone is severely malnourished at home</b>
Mortality 1/6	<b>Household has lost two or more children</b>
Electricity 1/18	The household has no electricity (No change)
Sanitation 1/18	<b>No facility available</b> so practice open defecation
Water 1/18	<b>No Safe water or a 45 minute walk</b>
Floor 1/18	The household has a dirt, sand, or dung floor (No change)
Fuel 1/18	<b>Cooks with Wood or Dung</b>
Assets 1/18	<b>Owns No Assets – Radio, television, mobile phone, bicycle etc.</b>

**Any person who is deprived in 1/3 of these weighted indicators is Destitute.**

# Overview

**Over half** of all MPI poor people are destitute.

**28 countries reduced destitution** (0.05); 29 reduced  $H^D$

**Largest reductions** in: Ethiopia, Niger, Ghana, Bolivia, Rwanda, Tanzania, Nepal, Haiti, Bangladesh (2004-7) and Zambia.

These are **LDCs** or **LICS** except Ghana & Bangladesh

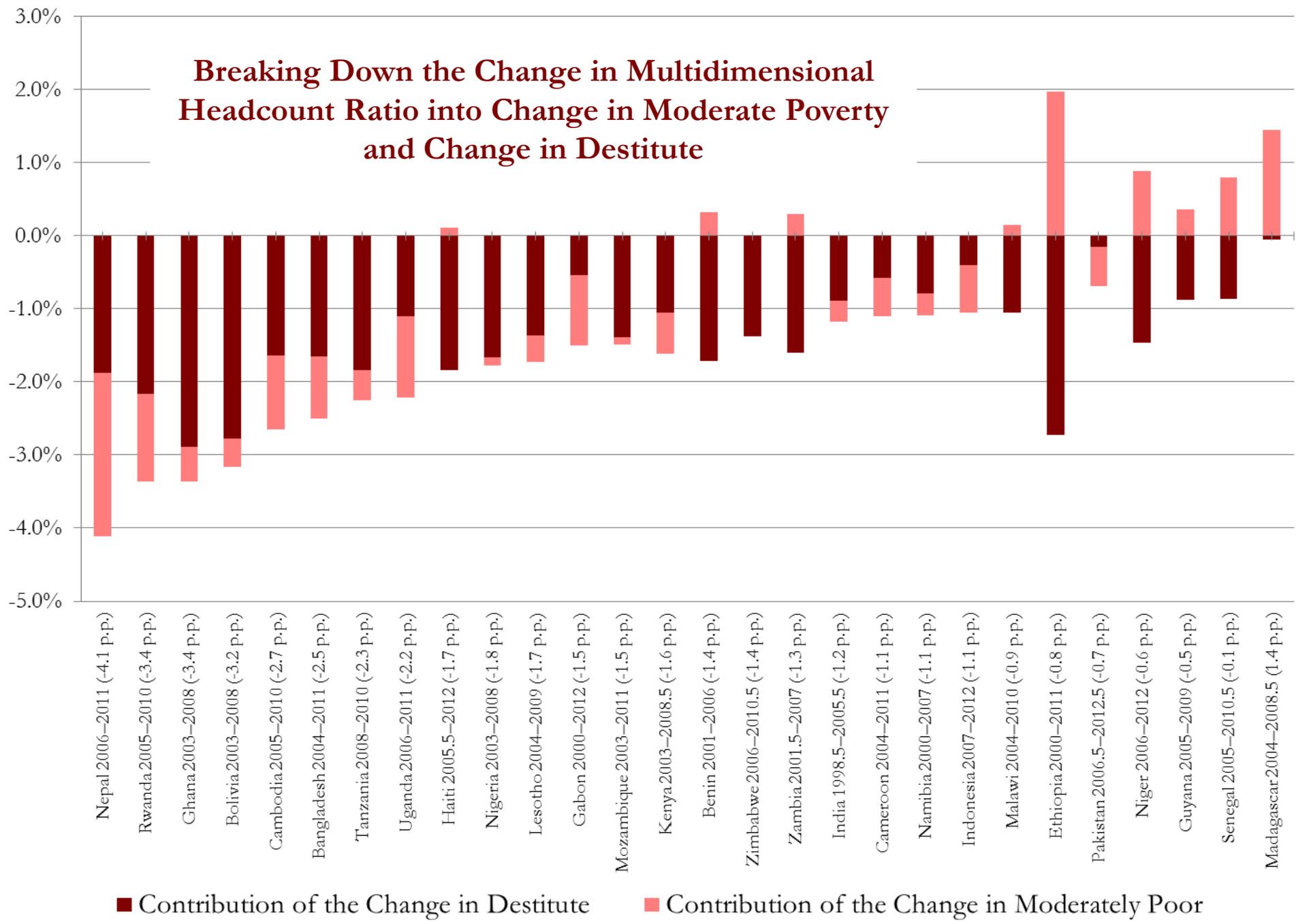
# Overview

In most countries, destitution is being reduced **faster than MPI** in relative terms; in 4 countries this is also true in absolute terms.

**Nine countries** reduced all destitution indicators significantly: Cambodia, Dominican Republic, Ethiopia (2000-5), Haiti, India, Indonesia, Mozambique, Niger and Rwanda (0.05).

27 countries had significant reductions of destitution in **rural** areas, and 20 countries in **urban** areas.

## Breaking Down the Change in Multidimensional Headcount Ratio into Change in Moderate Poverty and Change in Destitute

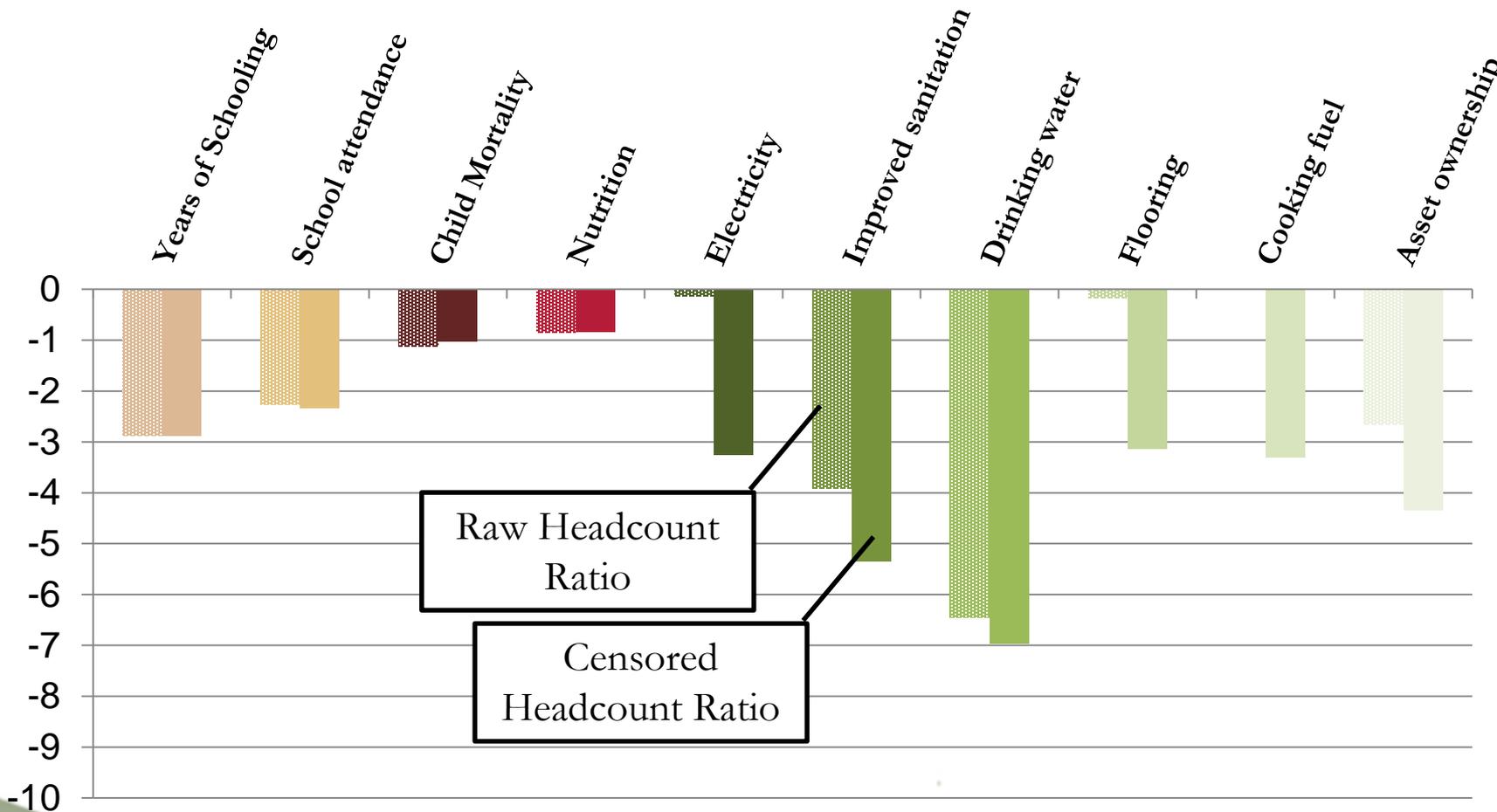


# Ethiopia: Reduction of Destitution

		National		Urban		Rural	
		Level	Annualised Change	Level	Annualised Change	Level	Annualised Change
MPI <sup>D</sup>	2000	.471	-	.115	-	.530	-
	2005	.339	-0.26***	.055	-.012***	.377	-.031***
	2011	.248	-0.015***	.054	-0.000	.290	-0.014***
Headcount Ratio	2000	82.1	-	25.9	-	91.4	-
	2005	65.4	-3.3***	12.7	-2.6***	72.6	-3.8***
	2011	52.1	-2.2***	12.9	.0	60.7	-2.0***
Average Intensity	2000	57.4	-	44.4	-	58.0	-
	2005	51.8	-1.1***	43.5	-0.2	52.0	-1.2***
	2011	47.6	-0.7***	42.1	-0.2	47.8	-0.7***

# Destitution in Ethiopia 2000 - 2005

Absolute Change in Headcount



Raw Headcount Ratio

Censored Headcount Ratio

# Conclusions

- ✓ Systemic account of multidimensional poverty dynamics using AF Adjusted Headcount Ratio and its consistent sub-indices
- ✓ 31 out of the 34 countries under study significantly reduced multidimensional poverty over two or three periods
- ✓ Variable relationships between the pace of multidimensional poverty reduction and reduction in \$1.25/day poverty require further study.
- ✓ Rather than theoretical or Shapley decompositions we simply study absolute changes in H and A at this point to avoid overly precise assumptions.
- ✓ Subnationally 208 regions had statistically significance reduction in MPI.
- ✓ There were significant changes in all of the ten MPI indicators, although the dimensional reduction profile varied across country.
- ✓ Destitution affected a disturbing proportion of the MPI poor, pointing to the need to explore ordinal 'depth' or at least subsets of the poor further.
- ✓ Destitution dynamics did not mirror MPI reduction, and were strongest in LICS and LDCs.